

# M.Sc., MATHEMATICS

## Syllabus

Program Code: PMT

2024 - Onwards



**MANNAR THIRUMALAI NAICKER COLLEGE**

(AUTONOMOUS)

Re-accredited with “A” Grade by NAAC

PASUMALAI, MADURAI – 625 004

**MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS),  
MADURAI – 625 004**

**M. SC MATHEMATICS CURRICULUM**

*(For the students admitted from the academic year 2024-2025 onwards)*

Course Code	Title of the Course	Hrs	Credits	Maximum Marks		
				Int	Ext	Total
<b>FIRST SEMESTER</b>						
<b>Part – III</b>	<b>Core courses</b>					
24PMTCC11	ALGEBRAIC STRUCTURES	<b>6</b>	<b>5</b>	<b>25</b>	<b>75</b>	<b>100</b>
24PMTCC12	REAL ANALYSIS - I	<b>6</b>	<b>5</b>	<b>25</b>	<b>75</b>	<b>100</b>
24PMTCC13	ORDINARY DIFFERENTIAL EQUATIONS	<b>6</b>	<b>4</b>	<b>25</b>	<b>75</b>	<b>100</b>
<b>Part – III</b>	<b>Elective courses</b>					
24PMTEC11	GRAPH THEORY AND APPLICATIONS	<b>6</b>	<b>3</b>	<b>25</b>	<b>75</b>	<b>100</b>
24PMTEC12	FUZZY SETS AND THEIR APPLICATIONS	<b>6</b>	<b>3</b>	<b>25</b>	<b>75</b>	<b>100</b>
<b>Total</b>		<b>30</b>	<b>20</b>	<b>125</b>	<b>375</b>	<b>500</b>
<b>SECOND SEMESTER</b>						
<b>Part – III</b>	<b>Core courses</b>					
24PMTCC21	ADVANCED ALGEBRA	<b>6</b>	<b>5</b>	<b>25</b>	<b>75</b>	<b>100</b>
24PMTCC22	REAL ANALYSIS - II	<b>6</b>	<b>5</b>	<b>25</b>	<b>75</b>	<b>100</b>
24PMTCC23	PARTIAL DIFFERENTIAL EQUATIONS	<b>6</b>	<b>4</b>	<b>25</b>	<b>75</b>	<b>100</b>
<b>Part – III</b>	<b>Elective courses</b>					
24PMTEC21	NUMERICAL ANALYSIS	<b>5</b>	<b>3</b>	<b>25</b>	<b>75</b>	<b>100</b>
24PMTEC22	RESOURCE MANAGEMENT TECHNIQUES	<b>5</b>	<b>3</b>	<b>25</b>	<b>75</b>	<b>100</b>
24PMTSP21	MATHEMATICS USING PYTHON	<b>2</b>	<b>2</b>	<b>25</b>	<b>75</b>	<b>100</b>
<b>Total</b>		<b>30</b>	<b>22</b>	<b>125</b>	<b>375</b>	<b>500</b>

# FIRST SEMESTER



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	ALGEBRAIC STRUCTURES			
<b>Course Code</b>	24PMTCC11	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	CORE	6	-	5
<b>COURSE OBJECTIVES:</b>				
▶ To introduce the concepts and to develop working knowledge on class equation, solvability of groups, finite abelian groups, linear transformations, real quadratic forms				
<b>UNIT – I</b>				<b>18</b>
Counting Principle - Class equation for finite groups and its applications - Sylow's theorems (For theorem 2.12.1, First proof only).				
<b>UNIT – II</b>				<b>18</b>
Solvable groups - Direct products - Finite abelian groups- Modules				
<b>UNIT - III</b>				<b>18</b>
Linear Transformations: Canonical forms –Triangular form - Nilpotent transformations.				
<b>UNIT – IV</b>				<b>18</b>
Jordan form - rational canonical form				
<b>UNIT - V</b>				<b>18</b>
Trace and transpose - Hermitian, unitary, normal transformations, real quadratic form.				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

- I.N. Herstein. *Topics in Algebra* (II Edition) Wiley Eastern Limited, New Delhi, 1975.

**UNIT-I : Chapter 2: Sections 2.11 and 2.12 (Omit Lemma 2.12.5)**

**UNIT-II : Chapter 5 : Section 5.7 (Lemma 5.7.1, Lemma 5.7.2, Theorem 5.7.1)**

**Chapter 2: Section 2.13 and 2.14 (Theorem 2.14.1 only)**

**Chapter 4: Section 4.5**

**UNIT-III: Chapter 6: Sections 6.4, 6.5**

**UNIT-IV : Chapter 6 : Sections 6.6 and 6.7**

**UNIT-V: Chapter 6 : Sections 6.8, 6.10 and 6.11 (Omit 6.9)**

**BOOKS FOR REFERENCES:**

- M.Artin, *Algebra*, Prentice Hall of India, 1991.
- P.B.Bhattacharya, S.K.Jain, and S.R.Nagpaul, *Basic Abstract Algebra* (II Edition) Cambridge University Press, 1997. (Indian Edition)
- I.S.Luther and I.B.S.Passi, *Algebra*, Vol. I –Groups(1996); Vol. II Rings, Narosa Publishing House , New Delhi, 1999
- D.S.Malik, J.N. Mordeson and M.K.Sen, *Fundamental of Abstract Algebra*, McGraw Hill (International Edition), New York. 1997.
- N.Jacobson, *Basic Algebra*, Vol. I & II W.H.Freeman (1980); also published by Hindustan Publishing Company, New Delhi.

**WEB RESOURCES:**

- ❖ <http://mathforum.org>, <http://ocw.mit.edu/ocwweb/Mathematics>,
- ❖ <http://www.opensource.org>,
- ❖ [www.algebra.com](http://www.algebra.com)

<b>Nature of Course</b>	EMPLOYABILITY	✓	SKILL ORIENTED		ENTREPRENEURSHIP	
<b>Curriculum Relevance</b>	LOCAL		REGIONAL		NATIONAL	✓ GLOBAL
<b>Changes Made in the Course</b>	Percentage of Change		No Changes Made		✓	New Course
<b>* Treat 20% as each unit (20*5=100%) and calculate the percentage of change for the course.</b>						

<b>COURSE OUTCOMES:</b>		<b>K LEVEL</b>
<b>After studying this course, the students will be able to:</b>		
<b>CO1</b>	Recall basic counting principle, define class equations to solve problems, explain Sylow's theorems and apply the theorem to find number of Sylow subgroups	<b>K1 to K5</b>
<b>CO2</b>	Define Solvable groups, define direct products, examine the properties of finite abelian groups, define modules	<b>K1 to K5</b>
<b>CO3</b>	Define similar Transformations, define invariant subspace, explore the properties of triangular matrix, to find the index of nilpotence to decompose a space into invariant subspaces, to find invariants of linear transformation, to explore the properties of nilpotent transformation relating nilpotence with invariants.	<b>K1 to K5</b>
<b>CO4</b>	Define Jordan, canonical form, Jordan blocks, define rational canonical form, define companion matrix of polynomial, find the elementary devices of transformation, and apply the concepts to find characteristic polynomial of linear transformation.	<b>K1 to K5</b>
<b>CO5</b>	Define trace, define transpose of a matrix, explain the properties of trace and transpose, to find trace, to find transpose of matrix, to prove Jacobson lemma using the triangular form, define symmetric matrix, skew symmetric matrix, adjoint, to define Hermitian, unitary, normal transformations and to verify whether the transformation in Hermitian, unitary and normal	<b>K1 to K5</b>

<b>MAPPING WITH PROGRAM OUTCOMES:</b>										
<b>CO/PO</b>	<b>PO1</b>	<b>PO2</b>	<b>PO3</b>	<b>PO4</b>	<b>PO5</b>	<b>PO6</b>	<b>PO7</b>	<b>PO8</b>	<b>PO9</b>	<b>PO10</b>
<b>CO1</b>	<b>3</b>	<b>1</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>3</b>				
<b>CO2</b>	<b>2</b>	<b>1</b>	<b>3</b>	<b>1</b>	<b>3</b>	<b>3</b>				
<b>CO3</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>1</b>	<b>3</b>	<b>3</b>				
<b>CO4</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>3</b>				
<b>CO5</b>	<b>3</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>3</b>				

**S- STRONG**

**M – MEDIUM**

**L - LOW**

<b>CO / PO MAPPING:</b>					
<b>COS</b>	<b>PSO1</b>	<b>PSO2</b>	<b>PSO3</b>	<b>PSO4</b>	<b>PSO5</b>
<b>CO 1</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 2</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 3</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 4</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 5</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

**LESSON PLAN:**

UNIT	ALGEBRAIC STRUCTURES	HRS	PEDAGOGY
I	Counting Principle - Class equation for finite groups and its applications - Sylow's theorems (For theorem 2.12.1, First proof only).	18	Chalk & Talk
II	Solvable groups - Direct products - Finite abelian groups- Modules	18	Chalk & Talk
III	Linear Transformations: Canonical forms –Triangular form - Nilpotent transformations	18	Chalk & Talk
IV	Jordan form - rational canonical form.	18	Chalk & Talk
V	Trace and transpose - Hermitian, unitary, normal transformations, real quadratic form.	18	Chalk & Talk

**Learning Outcome Based Education & Assessment (LOBE)  
Formative Examination - Blue Print  
Articulation Mapping – K Levels with Course Outcomes (COs)**

Internal	Cos	K Level	Section A		Section B Either or Choice	Section C Either or Choice
			MCQs			
			No. of Questions	K - Level		
CI	CO1	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AI	CO2	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
CI	CO3	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AII	CO4	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
Question Pattern CIA I & II		No. of Questions to be asked	4		4	4
		No. of Questions to be answered	4		2	2
		Marks for each question	1		5	8
		Total Marks for each section	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						



Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100

**NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.**

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions					
<b>PART – A</b>				<b>(10 x 1 = 10 Marks)</b>	
1.	<b>Unit - I</b>	<b>CO1</b>	<b>K1</b>	a)	b)
				c)	d)
2.	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>	a)	b)
				c)	d)
3.	<b>Unit - II</b>	<b>CO2</b>	<b>K1</b>	a)	b)
				c)	d)
4.	<b>Unit - II</b>	<b>CO2</b>	<b>K2</b>	a)	b)
				c)	d)
5.	<b>Unit - III</b>	<b>CO3</b>	<b>K1</b>	a)	b)
				c)	d)
6.	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	a)	b)
				c)	d)
7.	<b>Unit - IV</b>	<b>CO4</b>	<b>K1</b>	a)	b)
				c)	d)
8.	<b>Unit - IV</b>	<b>CO4</b>	<b>K2</b>	a)	b)
				c)	d)
9.	<b>Unit - V</b>	<b>CO5</b>	<b>K1</b>	a)	b)
				c)	d)
10.	<b>Unit - V</b>	<b>CO5</b>	<b>K2</b>	a)	b)
				c)	d)

Answer ALL the questions				PART – B	(5 x 5 = 25 Marks)
11. a)	Unit - I	CO1	K2		
OR					
11. b)	Unit - I	CO1	K2		
12. a)	Unit - II	CO2	K3		
OR					
12. b)	Unit - II	CO2	K3		
13. a)	Unit - III	CO3	K2		
OR					
13. b)	Unit - III	CO3	K2		
14. a)	Unit - IV	CO4	K3		
OR					
14. b)	Unit - IV	CO4	K3		
15. a)	Unit - V	CO5	K3		
OR					
15. b)	Unit - V	CO5	K3		

Answer ALL the questions				PART – C	(5 x 8 = 40 Marks)
16. a)	Unit - I	CO1	K3		
OR					
16. b)	Unit - I	CO1	K3		
17. a)	Unit - II	CO2	K4		
OR					
17. b)	Unit - II	CO2	K4		
18. a)	Unit - III	CO3	K3		
OR					
18. b)	Unit - III	CO3	K3		
19. a)	Unit - IV	CO4	K4		
OR					
19. b)	Unit - IV	CO4	K4		
20. a)	Unit - V	CO5	K4		
OR					
20. b)	Unit - V	CO5	K4		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	REAL ANALYSIS - I			
<b>Course Code</b>	24PMTCC12	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	CORE	6	-	5

### COURSE OBJECTIVES:

- To work comfortably with functions of bounded variation, Riemann-Stieltjes Integration, convergence of infinite series, infinite product and uniform convergence and its interplay between various limiting operations

### UNIT – I Functions of bounded variation & Infinite Series 18

Introduction - Properties of monotonic functions - Functions of bounded variation - Total variation - Additive property of total variation - Total variation on  $[a, x]$  as a function of  $x$  - Functions of bounded variation expressed as the difference of two increasing functions - Continuous functions of bounded variation.

Absolute and conditional convergence - Dirichlet's test and Abel's test - Rearrangement of series - Riemann's theorem on conditionally convergent series

### UNIT – II The Riemann - Stieltjes Integral 18

Introduction - Notation - The definition of the Riemann - Stieltjes integral - Linear Properties - Integration by parts- Change of variable in a Riemann - Stieltjes integral - Reduction to a Riemann Integral – Euler's summation formula - Monotonically increasing integrators, Upper and lower integrals - Additive and linearity properties of upper, lower integrals - Riemann's condition - Comparison theorems.

### UNIT - III The Riemann-Stieltjes Integral 18

Integrators of bounded variation-Sufficient conditions for the existence of Riemann-Stieltjes integrals- Necessary conditions for the existence of RS integrals- Mean value theorems -integrals as a function of the interval – Second fundamental theorem of integral calculus-Change of variable -Second Mean Value Theorem for Riemann integral- Riemann-Stieltjes integrals depending on a parameter- Differentiation under integral sign-Lebesgue criteriaon for existence of Riemann integrals.

### UNIT – IV Infinite Series and infinite Products & Power series 18

Double sequences - Double series - Rearrangement theorem for double series - A sufficient condition for equality of iterated series - Multiplication of series – Cesaro summability - Infinite products.

Multiplication of power series - The Taylor's series generated by a function - Bernstein's theorem - Abel's limit theorem - Tauber's theorem

**UNIT - V Sequences of Functions****18**

Pointwise convergence of sequences of functions - Examples of sequences of real - valued functions - Uniform convergence and continuity - Cauchy condition for uniform convergence - Uniform convergence of infinite series of functions - Riemann - Stieltjes integration – Non-uniform Convergence and Term-by-term Integration - Uniform convergence and differentiation - Sufficient condition for uniform convergence of a series - Mean convergence.

**Total Lecture Hours****90****BOOKS FOR STUDY:**

- Tom M.Apostol : *Mathematical Analysis*, 2<sup>nd</sup> Edition, Addison-Wesley Publishing Company Inc. New York, 1974

**UNIT I: Chapter – 6 : Sections 6.1 to 6.8****Chapter 8 : Sections 8.8, 8.15, 8.17, 8.18****UNIT II; Chapter - 7 : Sections 7.1 to 7.14****UNIT-III : Chapter - 7 : 7.15 to 7.26****UNIT-IV : Chapter - 8 Sec, 8.20, 8.21 to 8.26****Chapter 9 : Sections 9.14 9.15, 9.19, 9.20, 9.22, 9.23****UNIT-V: Chapter -9 Sec 9.1 to 9.6, 9.8,9.9,9.10,9.11, 9.13****BOOKS FOR REFERENCES:**

- Bartle, R.G. Real Analysis, John Wiley and Sons Inc., 1976.
- 2. Rudin,W. Principles of Mathematical Analysis, 3<sup>rd</sup> Edition. McGraw Hill Company, New York, 1976.
- 3. Malik,S.C. and Savita Arora. Mathematical Analysis, Wiley Eastern Limited.New Delhi, 1991.
- 4. Sanjay Arora and Bansi Lal, Introduction to Real Analysis, Satya Prakashan, New Delhi, 1991.
- 5. Gelbaum, B.R. and J. Olmsted, Counter Examples in Analysis, Holden day, San Francisco, 1964.
- 6. A.L.Gupta and N.R.Gupta, Principles of Real Analysis, Pearson Education, (Indian print) 2003.

**WEB RESOURCES:**

- ❖ <http://mathforum.org>, <http://ocw.mit.edu/ocwweb/Mathematics>,
- ❖ <http://www.opensource.org>, [www.mathpages.com](http://www.mathpages.com)

<b>Nature of Course</b>	EMPLOYABILITY	✓	SKILL ORIENTED	ENTREPRENEURSHIP
<b>Curriculum Relevance</b>	LOCAL	REGIONAL	NATIONAL	✓ GLOBAL
<b>Changes Made in the Course</b>	Percentage of Change	No Changes Made	✓	New Course
<b>* Treat 20% as each unit (20*5=100%) and calculate the percentage of change for the course.</b>				

<b>COURSE OUTCOMES:</b>		<b>K LEVEL</b>
<b>After studying this course, the students will be able to:</b>		
<b>CO1</b>	Analyze and evaluate functions of bounded variation and Rectifiable Curves.	<b>K1 to K5</b>
<b>CO2</b>	Describe the concept of Riemann-Stieltjes integral and its properties.	<b>K1 to K5</b>
<b>CO3</b>	Demonstrate the concept of step function, upper function, Lebesgue function and their integrals.	<b>K1 to K5</b>
<b>CO4</b>	Construct various mathematical proofs using the properties of Lebesgue integrals and establish the Levi monotone convergence theorem.	<b>K1 to K5</b>
<b>CO5</b>	Formulate the concept and properties of inner products, norms and measurable functions.	<b>K1 to K5</b>

<b>MAPPING WITH PROGRAM OUTCOMES:</b>										
CO/PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	3	1	3	2	3	3				
CO2	2	1	3	1	3	3				
CO3	3	2	3	1	3	3				
CO4	1	2	3	2	3	3				
CO5	3	1	2	3	3	3				

**S- STRONG**

**M – MEDIUM**

**L - LOW**

<b>CO / PO MAPPING:</b>					
COS	PSO1	PSO2	PSO3	PSO4	PSO5
CO 1	3	2	1		
CO 2	3	2	1		
CO 3	3	2	1		
CO 4	3	2	1		
CO 5	3	2	1		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

**LESSON PLAN:**

<b>UNIT</b>	<b>REAL ANALYSIS - I</b>	<b>HRS</b>	<b>PEDAGOGY</b>
<b>I</b>	Introduction - Properties of monotonic functions - Functions of bounded variation - Total variation - Additive property of total variation - Total variation on $[a, x]$ as a function of $x$ - Functions of bounded variation expressed as the difference of two increasing functions - Continuous functions of bounded variation. Absolute and conditional convergence - Dirichlet's test and Abel's test - Rearrangement of series - Riemann's theorem on conditionally convergent series.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>II</b>	Introduction - Notation - The definition of the Riemann - Stieltjes integral - Linear Properties - Integration by parts- Change of variable in a Riemann - Stieltjes integral - Reduction to a Riemann Integral – Euler's summation formula - Monotonically increasing integrators, Upper and lower integrals - Additive and linearity properties of upper, lower integrals - Riemann's condition - Comparison theorems.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>III</b>	Integrators of bounded variation-Sufficient conditions for the existence of Riemann-Stieltjes integrals-Necessary conditions for the existence of RS integrals- Mean value theorems -integrals as a function of the interval – Second fundamental theorem of integral calculus-Change of variable -Second Mean Value Theorem for Riemann integral- Riemann-Stieltjes integrals depending on a parameter- Differentiation under integral sign-Lebesgue criteriaon for existence of Riemann integrals.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>IV</b>	Double sequences - Double series - Rearrangement theorem for double series - A sufficient condition for equality of iterated series - Multiplication of series – Cesaro summability - Infinite products. Double sequences - Double series - Rearrangement theorem for double series - A sufficient condition for equality of iterated series - Multiplication of series – Cesaro summability - Infinite products.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>V</b>	Pointwise convergence of sequences of functions - Examples of sequences of real - valued functions - Uniform convergence and continuity - Cauchy condition for uniform convergence - Uniform convergence of infinite series of functions - Riemann - Stieltjes integration – Non-uniform Convergence and Term-by-term Integration - Uniform convergence and differentiation - Sufficient condition for uniform convergence of a series - Mean convergence.	<b>18</b>	<b>Chalk &amp; Talk</b>

**Learning Outcome Based Education & Assessment (LOBE)  
Formative Examination - Blue Print  
Articulation Mapping – K Levels with Course Outcomes (COs)**

Internal	Cos	K Level	Section A		Section B Either or Choice	Section C Either or Choice
			MCQs			
			No. of Questions	K - Level		
CI	CO1	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AI	CO2	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
CI	CO3	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AII	CO4	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
Question Pattern CIA I & II		No. of Questions to be asked	4		4	4
		No. of Questions to be answered	4		2	2
		Marks for each question	1		5	8
		Total Marks for each section	4		10	16

**Distribution of Marks with K Level CIA I & CIA II**

	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

<b>Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)</b>						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
<b>No. of Questions to be Asked</b>			10		10	10
<b>No. of Questions to be answered</b>			10		10	5
<b>Marks for each question</b>			1		1	8
<b>Total Marks for each section</b>			10		10	40
<b>(Figures in parenthesis denotes, questions should be asked with the given K level)</b>						

<b>Distribution of Marks with K Level</b>						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100
<b>NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.</b>						

### **Summative Examinations - Question Paper – Format**



Q. No.	Unit	CO	K-level		
Answer ALL the questions			<b>PART – A</b>		<b>(10 x 1 = 10 Marks)</b>
1.	<b>Unit - I</b>	<b>CO1</b>	<b>K1</b>		
				a)	b)
				c)	d)
2.	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>		
				a)	b)
				c)	d)
3.	<b>Unit - II</b>	<b>CO2</b>	<b>K1</b>		
				a)	b)
				c)	d)
4.	<b>Unit - II</b>	<b>CO2</b>	<b>K2</b>		
				a)	b)
				c)	d)
5.	<b>Unit - III</b>	<b>CO3</b>	<b>K1</b>		
				a)	b)
				c)	d)
6.	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>		
				a)	b)
				c)	d)
7.	<b>Unit - IV</b>	<b>CO4</b>	<b>K1</b>		
				a)	b)
				c)	d)
8.	<b>Unit - IV</b>	<b>CO4</b>	<b>K2</b>		
				a)	b)
				c)	d)
9.	<b>Unit - V</b>	<b>CO5</b>	<b>K1</b>		
				a)	b)
				c)	d)
10.	<b>Unit - V</b>	<b>CO5</b>	<b>K2</b>		
				a)	b)
				c)	d)

Answer ALL the questions				PART – B	(5 x 5 = 25 Marks)
11. a)	Unit - I	CO1	K2		
OR					
11. b)	Unit - I	CO1	K2		
12. a)	Unit - II	CO2	K3		
OR					
12. b)	Unit - II	CO2	K3		
13. a)	Unit - III	CO3	K2		
OR					
13. b)	Unit - III	CO3	K2		
14. a)	Unit - IV	CO4	K3		
OR					
14. b)	Unit - IV	CO4	K3		
15. a)	Unit - V	CO5	K3		
OR					
15. b)	Unit - V	CO5	K3		

Answer ALL the questions				PART – C	(5 x 8 = 40 Marks)
16. a)	Unit - I	CO1	K3		
OR					
16. b)	Unit - I	CO1	K3		
17. a)	Unit - II	CO2	K4		
OR					
17. b)	Unit - II	CO2	K4		
18. a)	Unit - III	CO3	K3		
OR					
18. b)	Unit - III	CO3	K3		
19. a)	Unit - IV	CO4	K4		
OR					
19. b)	Unit - IV	CO4	K4		
20. a)	Unit - V	CO5	K4		
OR					
20. b)	Unit - V	CO5	K4		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	ORDINARY DIFFERENTIAL EQUATIONS			
<b>Course Code</b>	24PMTCC13	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	CORE	6	-	4
<b>COURSE OBJECTIVES:</b>				
➤ To develop strong background on finding solutions to linear differential equations with constant and variable coefficients and also with singular points, to study existence and uniqueness of the solutions of first order differential equations				
<b>UNIT – I Linear equations with constant coefficients</b>				<b>18</b>
Second order homogeneous equations-Initial value problems-Linear dependence and independence-Wronskian and a formula for Wronskian-Non-homogeneous equation of order two.				
<b>UNIT – II Linear equations with constant coefficients</b>				<b>18</b>
Homogeneous and non-homogeneous equation of order n –Initial value problems- Annihilator method to solve non-homogeneous equation- Algebra of constant coefficient operators.				
<b>UNIT - III Linear equation with variable coefficients</b>				<b>18</b>
Initial value problems -Existence and uniqueness theorems – Solutions to solve a non-homogeneous equation – Wronskian and linear dependence – reduction of the order of a homogeneous equation – homogeneous equation with analytic coefficients-The Legendre equation				
<b>UNIT – IV Linear equation with regular singular point</b>				<b>18</b>
Euler equation – Second order equations with regular singular points –Exceptional cases – Bessel Function.				
<b>UNIT - V</b>				<b>18</b>
Existence and uniqueness of solutions to first order equations: Equation with variable separated – Exact equation – method of successive approximations – the Lipschitz condition – convergence of the successive approximations and the existence theorem.				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

- E.A.Coddington, A introduction to ordinary differential equations (3<sup>rd</sup> Printing) Prentice-Hall of India Ltd., New Delhi, 1987.

**Unit I - Chapter 2 : Section 1 to 6**

**Unit II - Chapter 2 : Section 7 to 12**

**Unit III - Chapter 3: Section 1 to 8**

**Unit IV - Chapter 4: Section 1 to 8**

**Unit V - Chapter 5: Section 1 to 8**

**BOOKS FOR REFERENCES:**

- Williams E. Boyce and Richard C. DI Prima, *Elementary differential equations and boundary value problems*, John Wiley and sons, New York, 1967.
- George F Simmons, *Differential equations with applications and historical notes*, Tata McGraw Hill, New Delhi, 1974.
- N.N. Lebedev, *Special functions and their applications*, Prentice Hall of India, New Delhi, 1965.
- W.T. Reid. *Ordinary Differential Equations*, John Wiley and Sons, New York, 1971
- M.D.Raisinghania, *Advanced Differential Equations*, S.Chand & Company Ltd. New Delhi 2001
- B.Rai, D.P.Choudary and H.I. Freedman, *A Course in Ordinary Differential Equations*, Narosa Publishing House, New Delhi, 2002.

**WEB RESOURCES:**

- ❖ <http://mathforum.org>,
- ❖ <http://ocw.mit.edu/ocwweb/Mathematics>,
- ❖ <http://www.opensource.org>,
- ❖ [www.mathpages.com](http://www.mathpages.com)

<b>Nature of Course</b>	EMPLOYABILITY	✓	SKILL ORIENTED		ENTREPRENEURSHIP			
<b>Curriculum Relevance</b>	LOCAL		REGIONAL		NATIONAL	✓	GLOBAL	
<b>Changes Made in the Course</b>	Percentage of Change			No Changes Made		✓	New Course	
<b>* Treat 20% as each unit (20*5=100%) and calculate the percentage of change for the course.</b>								

COURSE OUTCOMES:		K LEVEL
After studying this course, the students will be able to:		
CO1	Establish the qualitative behavior of solutions of systems of differential equations.	K1 to K5
CO2	Recognize the physical phenomena modeled by differential equations and dynamical systems.	K1 to K5
CO3	Analyze solutions using appropriate methods and give examples.	K1 to K5
CO4	Formulate Green's function for boundary value problems.	K1 to K5
CO5	Understand and use various theoretical ideas and results that underlie the mathematics in this course.	K1 to K5

MAPPING WITH PROGRAM OUTCOMES:										
CO/PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	3	1	3	2	3	3				
CO2	2	1	3	1	3	3				
CO3	3	2	3	1	3	3				
CO4	1	2	3	2	3	3				
CO5	3	1	2	3	3	3				
<b>S- STRONG</b>			<b>M – MEDIUM</b>				<b>L - LOW</b>			

CO / PO MAPPING:						
COS	PSO1	PSO2	PSO3	PSO4	PSO5	
CO 1	3	2	1			
CO 2	3	2	1			
CO 3	3	2	1			
CO 4	3	2	1			
CO 5	3	2	1			
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>			
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>			

LESSON PLAN:			
UNIT	ORDINARY DIFFERENTIAL EQUATIONS	HRS	PEDAGOGY
I	Second order homogeneous equations-Initial value problems-Linear dependence and independence-Wronskian and a formula for Wronskian-Non-homogeneous equation of order two.	18	Chalk & Talk
II	Homogeneous and non-homogeneous equation of order n –Initial value problems- Annihilator method to solve non-homogeneous equation-	18	Chalk & Talk

	Algebra of constant coefficient operators.		
<b>III</b>	Initial value problems -Existence and uniqueness theorems – Solutions to solve a non-homogeneous equation – Wronskian and linear dependence – reduction of the order of a homogeneous equation – homogeneous equation with analytic coefficients-The Legendre equation.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>IV</b>	Euler equation – Second order equations with regular singular points – Exceptional cases – Bessel Function.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>V</b>	Existence and uniqueness of solutions to first order equations: Equation with variable separated – Exact equation – method of successive approximations – the Lipschitz condition – convergence of the successive approximations and the existence theorem.	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>Learning Outcome Based Education &amp; Assessment (LOBE)</b>						
<b>Formative Examination - Blue Print</b>						
<b>Articulation Mapping – K Levels with Course Outcomes (COs)</b>						
<b>Internal</b>	<b>Cos</b>	<b>K Level</b>	<b>Section A</b>		<b>Section B Either or Choice</b>	<b>Section C Either or Choice</b>
			<b>MCQs</b>			
			<b>No. of Questions</b>	<b>K - Level</b>		
<b>CI</b>	<b>CO1</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AI</b>	<b>CO2</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>CI</b>	<b>CO3</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AII</b>	<b>CO4</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>Question Pattern CIA I &amp; II</b>		<b>No. of Questions to be asked</b>	4		4	4
		<b>No. of Questions to be answered</b>	4		2	2
		<b>Marks for each question</b>	1		5	8
		<b>Total Marks for each section</b>	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100

**NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.**

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions				<b>PART – A</b>	
				<b>(10 x 1 = 10 Marks)</b>	
1.	<b>Unit - I</b>	<b>CO1</b>	<b>K1</b>	a)	b)
				c)	d)
2.	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>	a)	b)
				c)	d)
3.	<b>Unit - II</b>	<b>CO2</b>	<b>K1</b>	a)	b)
				c)	d)
4.	<b>Unit - II</b>	<b>CO2</b>	<b>K2</b>	a)	b)
				c)	d)
5.	<b>Unit - III</b>	<b>CO3</b>	<b>K1</b>	a)	b)
				c)	d)
6.	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	a)	b)
				c)	d)
7.	<b>Unit - IV</b>	<b>CO4</b>	<b>K1</b>	a)	b)
				c)	d)
8.	<b>Unit - IV</b>	<b>CO4</b>	<b>K2</b>	a)	b)
				c)	d)
9.	<b>Unit - V</b>	<b>CO5</b>	<b>K1</b>	a)	b)
				c)	d)
10.	<b>Unit - V</b>	<b>CO5</b>	<b>K2</b>	a)	b)
				c)	d)



Answer ALL the questions				PART – B	(5 x 5 = 25 Marks)
11. a)	Unit - I	CO1	K2		
OR					
11. b)	Unit - I	CO1	K2		
12. a)	Unit - II	CO2	K3		
OR					
12. b)	Unit - II	CO2	K3		
13. a)	Unit - III	CO3	K2		
OR					
13. b)	Unit - III	CO3	K2		
14. a)	Unit - IV	CO4	K3		
OR					
14. b)	Unit - IV	CO4	K3		
15. a)	Unit - V	CO5	K3		
OR					
15. b)	Unit - V	CO5	K3		

Answer ALL the questions				PART – C	(5 x 8 = 40 Marks)
16. a)	Unit - I	CO1	K3		
OR					
16. b)	Unit - I	CO1	K3		
17. a)	Unit - II	CO2	K4		
OR					
17. b)	Unit - II	CO2	K4		
18. a)	Unit - III	CO3	K3		
OR					
18. b)	Unit - III	CO3	K3		
19. a)	Unit - IV	CO4	K4		
OR					
19. b)	Unit - IV	CO4	K4		
20. a)	Unit - V	CO5	K4		
OR					
20. b)	Unit - V	CO5	K4		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	GRAPH THEORY AND APPLICATIONS			
<b>Course Code</b>	24PMTEC11	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	ELECTIVE	6	-	3
<b>COURSE OBJECTIVES:</b>				
<ul style="list-style-type: none"><li>➤ To understand the fundamental concepts in graph theory.</li><li>➤ To apply graph theory in different fields</li><li>➤ To improve the different types of proof writing skills.</li><li>➤ To learn to model problems using graphs</li><li>➤ To solve the problems algorithmically.</li></ul>				
<b>UNIT – I</b>				<b>18</b>
The Incidence and Adjacency Matrices, Sub graphs, Vertex degrees, Paths and Connection, Cycles, Sperner's lemma, Trees, Cut edges and Bonds, Cut vertices				
<b>UNIT – II</b>				<b>18</b>
Euler tours, Hamiltonian cycles, The travelling salesman problem, Matchings, Matchings and Coverings in Bipartite graphs				
<b>UNIT - III</b>				<b>18</b>
Edge Chromatic Number, Vizing's Theorem, Chromatic number, Brook's theorem.				
<b>UNIT – IV</b>				<b>18</b>
Plane and Planar graphs, Dual Graphs ,Euler's formula ,Bridges ,Kuratowski's Theorem, Directed Graphs, Directed Paths, Directed Cycles, Flows, Cuts, The Max-Flow Min –Cut theorem				
<b>UNIT - V</b>				<b>18</b>
Algorithms : connectedness and components – spanning tree – cut vertices and separability – directed circuits – shortest path algorithm – planarity testing – isomorphism				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

➤ J.A.Bondy and U.S.R.Murty, Graph Theory with Applications. North Holland Publications, New york, 1976.

**Unit I - Chapter 1 : Section 1.3 to 1.7 and 1.9**

**Chapter 2: Section 2.1 to 2.3**

**Unit II – Chapter 4: Section 4.1, 4.2 and 4.4**

**Chapter 5: Section 5.1 to 5.2**

**Unit III - Chapter 6 : Section 6.1, 6.2**

**Chapter 8 : Section 8.1, 8.2**

**Unit IV - Chapter 9 : Section 9.1 to 9.5**

**Chapter 10 : Section 10.1 to 10.3**

➤ Narsingh Deo: Graph Theory with Applications to Engineering and Computer Science, Prentice Hall, 1979.

**Unit V - Chapter 11 : Section 11.4 to 11.7**

**BOOKS FOR REFERENCES:**

➤ John Clark and Derek Allan Holton, **A first look at Graph Theory**, World Scientific Publications, Singapore, 1991.

➤ Harary, **Graph Theory**, Narosa Publishing House, New Delhi, 1988.

➤ S.K.Yadav, **Elements of Graph Theory**, Ane Books Pvt. Ltd, New Delhi, 2010

**WEB RESOURCES:**

❖ <https://nptel.ac.in/courses/111/106/111106102/>

❖ <https://nptel.ac.in/courses/111/106/111106050/>

❖ [https://www.math.kit.edu/iag6/lehre/graphtheo2015w/media/lecture\\_notes.pdf](https://www.math.kit.edu/iag6/lehre/graphtheo2015w/media/lecture_notes.pdf)

<b>Nature of Course</b>	EMPLOYABILITY	✓	SKILL ORIENTED		ENTREPRENEURSHIP	
<b>Curriculum Relevance</b>	LOCAL		REGIONAL		NATIONAL	✓ GLOBAL
<b>Changes Made in the Course</b>	Percentage of Change		No Changes Made		✓	New Course

**\* Treat 20% as each unit (20\*5=100%) and calculate the percentage of change for the course.**

<b>COURSE OUTCOMES:</b>	<b>K LEVEL</b>
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After studying this course, the students will be able to:

<b>CO1</b>	Understand the definition of different types of graphs and Sperner’s lemma.	<b>K1 to K5</b>
<b>CO2</b>	Make use of graph theory concepts in travelling salesman problem, Matching and covering.	<b>K1 to K5</b>
<b>CO3</b>	Categorize chromatic number, edge chromatic number with theorems.	<b>K1 to K5</b>
<b>CO4</b>	Develop the different types of proof writing skills for planar graphs and directed graphs	<b>K1 to K5</b>
<b>CO5</b>	Apply various types of algorithms in graph.	<b>K1 to K5</b>

<b>MAPPING WITH PROGRAM OUTCOMES:</b>										
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<b>CO/PO</b>	<b>PO1</b>	<b>PO2</b>	<b>PO3</b>	<b>PO4</b>	<b>PO5</b>	<b>PO6</b>	<b>PO7</b>	<b>PO8</b>	<b>PO9</b>	<b>PO10</b>
<b>CO1</b>	<b>3</b>	<b>2</b>	<b>1</b>	-	-	<b>2</b>				
<b>CO2</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>1</b>	<b>2</b>	<b>1</b>				
<b>CO3</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>2</b>	-				
<b>CO4</b>	<b>3</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>				
<b>CO5</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>2</b>	<b>2</b>	<b>1</b>				

**S- STRONG**

**M – MEDIUM**

**L - LOW**

<b>CO / PO MAPPING:</b>						
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<b>COS</b>	<b>PSO1</b>	<b>PSO2</b>	<b>PSO3</b>	<b>PSO4</b>	<b>PSO5</b>
<b>CO 1</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 2</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 3</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 4</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 5</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

<b>LESSON PLAN:</b>			
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<b>UNIT</b>	<b>GRAPH THEORY AND APPLICATIONS</b>	<b>HRS</b>	<b>PEDAGOGY</b>
<b>I</b>	The Incidence and Adjacency Matrices, Sub graphs, Vertex degrees, Paths and Connection, Cycles, Sperner’s lemma, Trees, Cut edges and Bonds, Cut vertices	<b>18</b>	<b>PPT, Chalk &amp; Talk, quiz</b>
<b>II</b>	Euler tours, Hamiltonian cycles, The travelling salesman problem, Matchings, Matchings and Coverings in Bipartite graphs	<b>18</b>	<b>Chalk &amp; Talk, PPT</b>
<b>III</b>	Edge Chromatic Number, Vizing’s Theorem, Chromatic number, Brook’s theorem	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>IV</b>	Plane and Planar graphs, Dual Graphs ,Euler’s formula ,Bridges , Kuratowski’s Theorem, Directed Graphs, Directed Paths, Directed Cycles, Flows, Cuts, The Max-Flow Min –Cut theorem.	<b>18</b>	<b>Chalk &amp; Talk, Assignment</b>
<b>V</b>	Algorithms : connectedness and components – spanning tree – cut vertices and separability – directed circuits – shortest path algorithm – planarity testing – isomorphism	<b>18</b>	<b>Chalk &amp; Talk, PPT</b>

<b>Learning Outcome Based Education &amp; Assessment (LOBE)</b>						
<b>Formative Examination - Blue Print</b>						
<b>Articulation Mapping – K Levels with Course Outcomes (COs)</b>						
<b>Internal</b>	<b>Cos</b>	<b>K Level</b>	<b>Section A</b>		<b>Section B Either or Choice</b>	<b>Section C Either or Choice</b>
			<b>MCQs</b>			
			<b>No. of Questions</b>	<b>K - Level</b>		
<b>CI</b>	<b>CO1</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AI</b>	<b>CO2</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>CI</b>	<b>CO3</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AII</b>	<b>CO4</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>Question Pattern CIA I &amp; II</b>		<b>No. of Questions to be asked</b>	4		4	4
		<b>No. of Questions to be answered</b>	4		2	2
		<b>Marks for each question</b>	1		5	8
		<b>Total Marks for each section</b>	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100

**NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.**

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions				<b>PART – A</b>	
				<b>(10 x 1 = 10 Marks)</b>	
1.	Unit - I	CO1	K1	a)	b)
				c)	d)
2.	Unit - I	CO1	K2	a)	b)
				c)	d)
3.	Unit - II	CO2	K1	a)	b)
				c)	d)
4.	Unit - II	CO2	K2	a)	b)
				c)	d)
5.	Unit - III	CO3	K1	a)	b)
				c)	d)
6.	Unit - III	CO3	K2	a)	b)
				c)	d)
7.	Unit - IV	CO4	K1	a)	b)
				c)	d)
8.	Unit - IV	CO4	K2	a)	b)
				c)	d)
9.	Unit - V	CO5	K1	a)	b)
				c)	d)
10.	Unit - V	CO5	K2	a)	b)
				c)	d)

Answer ALL the questions				PART – B	(5 x 5 = 25 Marks)
11. a)	Unit - I	CO1	K2		
OR					
11. b)	Unit - I	CO1	K2		
12. a)	Unit - II	CO2	K3		
OR					
12. b)	Unit - II	CO2	K3		
13. a)	Unit - III	CO3	K2		
OR					
13. b)	Unit - III	CO3	K2		
14. a)	Unit - IV	CO4	K3		
OR					
14. b)	Unit - IV	CO4	K3		
15. a)	Unit - V	CO5	K3		
OR					
15. b)	Unit - V	CO5	K3		

Answer ALL the questions				PART – C	(5 x 8 = 40 Marks)
16. a)	Unit - I	CO1	K3		
OR					
16. b)	Unit - I	CO1	K3		
17. a)	Unit - II	CO2	K4		
OR					
17. b)	Unit - II	CO2	K4		
18. a)	Unit - III	CO3	K3		
OR					
18. b)	Unit - III	CO3	K3		
19. a)	Unit - IV	CO4	K4		
OR					
19. b)	Unit - IV	CO4	K4		
20. a)	Unit - V	CO5	K4		
OR					
20. b)	Unit - V	CO5	K4		





# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>COURSE NAME</b>	FUZZY SETS AND THEIR APPLICATIONS			
<b>COURSE CODE</b>	24PMTEC12	<b>L</b>	<b>P</b>	<b>C</b>
<b>CATEGORY</b>	ELECTIVE	6	-	3
<b>COURSE OBJECTIVES:</b>				
<ul style="list-style-type: none"><li>➤ To familiarize the concept of crisp set and its properties</li><li>➤ To learn the basics of fuzzy sets and its operations</li><li>➤ To differentiate crisp logic, multi-valued logic and fuzzy logic</li><li>➤ To use inference theory in fuzzy logic</li><li>➤ To learn the application in real life</li></ul>				
<b>UNIT – I</b>				<b>18</b>
Fuzzy sets: Basic types– Basic concepts – Additional properties of $\alpha$ – cuts – Representation of fuzzy sets – Extension principle for fuzzy sets – Types of operations – Fuzzy complements				
<b>UNIT – II</b>				<b>18</b>
Fuzzy numbers – Linguistic variables – Arithmetic operation on intervals – Arithmetic operation on fuzzy numbers				
<b>UNIT - III</b>				<b>18</b>
Fuzzy relation : Crisp versus Fuzzy relation – projection and cylindric extensions- Binary fuzzy relation on a single set – fuzzy equivalence relations – Fuzzy compatibility relation				
<b>UNIT – IV</b>				<b>18</b>
Fuzzy logic: Classical logic – An over view – multi valued logic – Fuzzy propositions –Fuzzy quantifiers – Linguistic hedges – Inference from conditional fuzzy propositions – Inference from conditional and quantified propositions – Inference from quantified propositions				
<b>UNIT - V</b>				<b>18</b>
Applications: Applications to Civil Engineering –Computer Engineering – Reliability theory – Robotics – Medicine – Economics.				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

- George J Klir and B.Yuan, **Fuzzy sets and Fuzzy logic – Theory and application**, Second edition, Prentice Hall, New Delhi, 1995.

Unit I - Chapter 1 : Sections 1.2 to 1.4  
 Chapter 2 : Sections 2.1 to 2.3  
 Chapter 3 : Sections 3.1,3.2  
 Unit II - Chapter 4 : Section 4.1 to 4.4  
 Unit III - Chapter 5 : Sections 5.1 to 5.6  
 Unit IV - Chapter 8 : Sections 8.2 to 8.8  
 Unit V - Chapter 16 : Sections 16.1 , 16.2, 16.5 to 16.7,  
 Chapter 17 : Sections 17.1 to 17.3.

**BOOKS FOR REFERENCES:**

- H.J.Zimmermann, **Fuzzy Set Theory and its Applications**, Fourth Edition, Springer Publishers, New Delhi, 2006.
- Timothy J. Ross, “**Fuzzy Logic with Engineering Applications**”, 3rd Edition, Wiley, 2010.
- Michal Baczynski and Balasubramaniam Jayaram, **Fuzzy Implications**, Springer Verlag, Heidelberg, 2008

**WEB RESOURCES:**

- ❖ <https://www.thesis scientist.com/docs/Study%20Notes/66860129-5a91-459d-810f-54e0fc41175d>
- ❖ <https://ocw.mit.edu/courses/health-sciences-and-technology/hst-951j-medical-decision-support-spring-2003/lecture-notes/lecture4.pdf>
- ❖ <https://www.iitk.ac.in/eeold/archive/courses/2013/intel-info/d1pdf3.pdf>
- ❖ <https://nptel.ac.in/courses/106105173/2>
- ❖ [https://www.cse.iitb.ac.in/~cs621-2011/lectures\\_2009/cs621-lect38-fuzzy-logic-2009-11-11.ppt](https://www.cse.iitb.ac.in/~cs621-2011/lectures_2009/cs621-lect38-fuzzy-logic-2009-11-11.ppt)

<b>Nature of Course</b>	EMPLOYABILITY	✓	SKILL ORIENTED		ENTREPRENEURSHIP	
<b>Curriculum Relevance</b>	LOCAL		REGIONAL		NATIONAL	✓ GLOBAL
<b>Changes Made in the Course</b>	Percentage of Change		No Changes Made		✓	New Course

**\* Treat 20% as each unit (20\*5=100%) and calculate the percentage of change for the course.**

<b>COURSE OUTCOMES:</b>	<b>K LEVEL</b>
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After studying this course, the students will be able to:

<b>CO1</b>	Interpret fuzzy set theory, representation, operation and extension principle	<b>K1 to K5</b>
<b>CO2</b>	Identify fuzzy numbers and its linguistic variables	<b>K1 to K5</b>
<b>CO3</b>	Validate fuzzy relation, projections and its equivalence.	<b>K1 to K5</b>
<b>CO4</b>	Analyse multi valued logic and fuzzy logic with inference theory	<b>K1 to K5</b>
<b>CO5</b>	Apply fuzziness in real valued problems	<b>K1 to K5</b>

<b>MAPPING WITH PROGRAM OUTCOMES:</b>										
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CO/PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
<b>CO1</b>	<b>3</b>	<b>2</b>	-	<b>1</b>	<b>2</b>	-				
<b>CO2</b>	<b>2</b>	<b>2</b>	-	-	<b>2</b>	-				
<b>CO3</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>1</b>				
<b>CO4</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>1</b>				
<b>CO5</b>	<b>2</b>	<b>1</b>	<b>1</b>	<b>1</b>	-	<b>2</b>				

**S- STRONG**

**M – MEDIUM**

**L - LOW**

<b>CO / PO MAPPING:</b>
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COS	PSO1	PSO2	PSO3	PSO4	PSO5
<b>CO 1</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 2</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 3</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 4</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 5</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

<b>LESSON PLAN:</b>
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<b>UNIT</b>	<b>FUZZY SETS AND THEIR APPLICATIONS</b>	<b>HRS</b>	<b>PEDAGOGY</b>
<b>I</b>	Fuzzy sets: Basic types– Basic concepts – Additional properties of $\alpha$ – cuts – Representation of fuzzy sets – Extension principle for fuzzy sets – Types of operations – Fuzzy complements	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>II</b>	Fuzzy numbers – Linguistic variables – Arithmetic operation on intervals – Arithmetic operation on fuzzy numbers	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>III</b>	Fuzzy relation : Crisp versus Fuzzy relation – projection and cylindric extensions- Binary fuzzy relation on a single set – fuzzy equivalence relations – Fuzzy compatibility relation	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>IV</b>	Fuzzy logic: Classical logic – An over view – multi valued logic – Fuzzy propositions –Fuzzy quantifiers – Linguistic hedges – Inference from conditional fuzzy propositions – Inference from conditional and quantified propositions – Inference from quantified propositions	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>V</b>	Applications: Applications to Civil Engineering –Computer Engineering – Reliability theory – Robotics – Medicine – Economics.	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>Learning Outcome Based Education &amp; Assessment (LOBE) Formative Examination - Blue Print Articulation Mapping – K Levels with Course Outcomes (COs)</b>						
<b>Internal</b>	<b>Cos</b>	<b>K Level</b>	<b>Section A</b>		<b>Section B Either or Choice</b>	<b>Section C Either or Choice</b>
			<b>MCQs</b>			
			<b>No. of Questions</b>	<b>K - Level</b>		
<b>CI</b>	<b>CO1</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AI</b>	<b>CO2</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>CI</b>	<b>CO3</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AII</b>	<b>CO4</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>Question Pattern CIA I &amp; II</b>		<b>No. of Questions to be asked</b>	4		4	4
		<b>No. of Questions to be answered</b>	4		2	2
		<b>Marks for each question</b>	1		5	8
		<b>Total Marks for each section</b>	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100

**NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.**

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions			PART – A		(10 x 1 = 10 Marks)
1.	Unit - I	CO1	K1	a)	b)
				c)	d)
2.	Unit - I	CO1	K2	a)	b)
				c)	d)
3.	Unit - II	CO2	K1	a)	b)
				c)	d)
4.	Unit - II	CO2	K2	a)	b)
				c)	d)
5.	Unit - III	CO3	K1	a)	b)
				c)	d)
6.	Unit - III	CO3	K2	a)	b)
				c)	d)
7.	Unit - IV	CO4	K1	a)	b)
				c)	d)
8.	Unit - IV	CO4	K2	a)	b)
				c)	d)
9.	Unit - V	CO5	K1	a)	b)
				c)	d)
10.	Unit - V	CO5	K2	a)	b)
				c)	d)

Answer ALL the questions				PART – B	(5 x 5 = 25 Marks)
11. a)	Unit - I	CO1	K2		
OR					
11. b)	Unit - I	CO1	K2		
12. a)	Unit - II	CO2	K3		
OR					
12. b)	Unit - II	CO2	K3		
13. a)	Unit - III	CO3	K2		
OR					
13. b)	Unit - III	CO3	K2		
14. a)	Unit - IV	CO4	K3		
OR					
14. b)	Unit - IV	CO4	K3		
15. a)	Unit - V	CO5	K3		
OR					
15. b)	Unit - V	CO5	K3		

Answer ALL the questions				PART – C	(5 x 8 = 40 Marks)
16. a)	Unit - I	CO1	K3		
OR					
16. b)	Unit - I	CO1	K3		
17. a)	Unit - II	CO2	K4		
OR					
17. b)	Unit - II	CO2	K4		
18. a)	Unit - III	CO3	K3		
OR					
18. b)	Unit - III	CO3	K3		
19. a)	Unit - IV	CO4	K4		
OR					
19. b)	Unit - IV	CO4	K4		
20. a)	Unit - V	CO5	K4		
OR					
20. b)	Unit - V	CO5	K4		

# SECOND SEMESTER





# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	ADVANCED ALGEBRA			
<b>Course Code</b>	24PMTCC21	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	CORE	6	-	5
<b>COURSE OBJECTIVES:</b>				
➤ To study field extension, roots of polynomials, Galois Theory, finite fields, division rings, solvability by radicals and to develop computational skill in abstract algebra.				
<b>UNIT - I</b>				<b>18</b>
Extension fields – Transcendence of $e$				
<b>UNIT - II</b>				<b>18</b>
Roots of Polynomials.- More about roots				
<b>UNIT - III</b>				<b>18</b>
Elements of Galois theory.				
<b>UNIT - IV</b>				<b>18</b>
Finite fields - Wedderburn's theorem on finite division rings.				
<b>UNIT - V</b>				<b>18</b>
Solvability by radicals - A theorem of Frobenius - Integral Quaternions and the Four - Square theorem				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

- I.N. Herstein. *Topics in Algebra* (II Edition) Wiley Eastern Limited, New Delhi, 1975.

**UNIT I: Chapter 5: Section 5.1 and 5.2**

**UNIT 2: Chapter 5: Sections 5.3 and 5.5**

**UNIT 3: Chapter 5 : Section 5.6**

**UNIT 4: Chapter 7: Sections 7.1 and 7.2 (Theorem 7.2.1 only)**

**UNIT 5: Chapter 5: Section 5.7 (omit Lemma 5.7.1, Lemma 5.7.2 and Theorem 5.7.1)**

**Chapter 7 : Sections 7.3 and 7.4**

**BOOKS FOR REFERENCES:**

- M.Artin, *Algebra*, Prentice Hall of India, 1991.
- P.B.Bhattacharya, S.K.Jain, and S.R.Nagpaul, *Basic Abstract Algebra* (II Edition) Cambridge University Press, 1997. (Indian Edition)
- I.S.Luther and I.B.S.Passi, *Algebra*, Vol. I –Groups(1996); Vol. II *Rings*, Narosa Publishing House , New Delhi, 1999
- D.S.Malik, J.N. Mordeson and M.K.Sen, *Fundamental of Abstract Algebra*, McGraw Hill (International Edition), New York. 1997.
- N.Jacobson, *Basic Algebra*, Vol. I & II Hindustan Publishing Company, New Delhi.

**WEB RESOURCES:**

- ❖ <http://mathforum.org>
- ❖ <http://ocw.mit.edu/ocwweb/Mathematics>,
- ❖ <http://www.opensource.org>,
- ❖ [www.algebra.com](http://www.algebra.com)

<b>Nature of Course</b>	EMPLOYABILITY	✓	SKILL ORIENTED		ENTREPRENEURSHIP			
<b>Curriculum Relevance</b>	LOCAL		REGIONAL		NATIONAL	✓	GLOBAL	
<b>Changes Made in the Course</b>	Percentage of Change		No Changes Made		✓	New Course		

**\* Treat 20% as each unit (20\*5=100%) and calculate the percentage of change for the course.**

<b>COURSE OUTCOMES:</b>	<b>K LEVEL</b>
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After studying this course, the students will be able to:

<b>CO1</b>	Prove theorems applying algebraic ways of thinking.	<b>K1 to K5</b>
<b>CO2</b>	Connect groups with graphs and understanding about Hamiltonian graphs.	<b>K1 to K5</b>
<b>CO3</b>	Compose clear and accurate proofs using the concepts of Galois Theory.	<b>K1 to K5</b>
<b>CO4</b>	Bring out insight into Abstract Algebra with focus on axiomatic theories.	<b>K1 to K5</b>
<b>CO5</b>	Demonstrate knowledge and understanding of fundamental concepts including extension fields, Algebraic extensions, Finite fields, Class equations and Sylow's theorem.	<b>K1 to K5</b>

<b>MAPPING WITH PROGRAM OUTCOMES:</b>										
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CO/PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	3	1	3	2	3	3				
CO2	2	1	3	1	3	3				
CO3	3	2	3	1	3	3				
CO4	1	2	3	2	3	3				
CO5	3	1	2	3	3	3				

**S- STRONG**

**M – MEDIUM**

**L - LOW**

<b>CO / PO MAPPING:</b>					
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COS	PSO1	PSO2	PSO3	PSO4	PSO5
CO 1	3	2	1		
CO 2	3	2	1		
CO 3	3	2	1		
CO 4	3	2	1		
CO 5	3	2	1		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

<b>LESSON PLAN:</b>			
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UNIT	ADVANCED ALGEBRA	HRS	PEDAGOGY
I	Extension fields – Transcendence of e.	<b>18</b>	<b>Chalk &amp; Talk</b>
II	Roots or Polynomials.- More about roots	<b>18</b>	<b>Chalk &amp; Talk</b>
III	Elements of Galois theory.	<b>18</b>	<b>Chalk &amp; Talk</b>
IV	Finite fields - Wedderburn's theorem on finite division rings.	<b>18</b>	<b>Chalk &amp;</b>

			<b>Talk</b>
<b>V</b>	Solvability by radicals - A theorem of Frobenius - Integral Quaternions and the Four - Square theorem.	<b>18</b>	<b>Chalk &amp; Talk</b>

Learning Outcome Based Education & Assessment (LOBE) Formative Examination - Blue Print Articulation Mapping – K Levels with Course Outcomes (COs)						
Internal	Cos	K Level	Section A		Section B Either or Choice	Section C Either or Choice
			MCQs			
			No. of Questions	K - Level		
CI	CO1	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AI	CO2	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
CI	CO3	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AII	CO4	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
Question Pattern CIA I & II		No. of Questions to be asked	4		4	4
		No. of Questions to be answered	4		2	2
		Marks for each question	1		5	8
		Total Marks for each section	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	
	K4			16	16	28.6	
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	
	K4		10	16	26	46.4	
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

<b>Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)</b>						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

<b>Distribution of Marks with K Level</b>						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100
<b>NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.</b>						

## Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions			<b>PART – A</b>		<b>(10 x 1 = 10 Marks)</b>
1.	<b>Unit - I</b>	<b>CO1</b>	<b>K1</b>		
				a)	b)
				c)	d)
2.	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>		
				a)	b)
				c)	d)
3.	<b>Unit - II</b>	<b>CO2</b>	<b>K1</b>		
				a)	b)
				c)	d)
4.	<b>Unit - II</b>	<b>CO2</b>	<b>K2</b>		
				a)	b)
				c)	d)
5.	<b>Unit - III</b>	<b>CO3</b>	<b>K1</b>		
				a)	b)
				c)	d)
6.	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>		
				a)	b)
				c)	d)
7.	<b>Unit - IV</b>	<b>CO4</b>	<b>K1</b>		
				a)	b)
				c)	d)
8.	<b>Unit - IV</b>	<b>CO4</b>	<b>K2</b>		
				a)	b)
				c)	d)
9.	<b>Unit - V</b>	<b>CO5</b>	<b>K1</b>		
				a)	b)
				c)	d)
10.	<b>Unit - V</b>	<b>CO5</b>	<b>K2</b>		
				a)	b)
				c)	d)

Answer ALL the questions				PART – B	(5 x 5 = 25 Marks)
11. a)	Unit - I	CO1	K2		
OR					
11. b)	Unit - I	CO1	K2		
12. a)	Unit - II	CO2	K3		
OR					
12. b)	Unit - II	CO2	K3		
13. a)	Unit - III	CO3	K2		
OR					
13. b)	Unit - III	CO3	K2		
14. a)	Unit - IV	CO4	K3		
OR					
14. b)	Unit - IV	CO4	K3		
15. a)	Unit - V	CO5	K3		
OR					
15. b)	Unit - V	CO5	K3		

Answer ALL the questions				PART – C	(5 x 8 = 40 Marks)
16. a)	Unit - I	CO1	K3		
OR					
16. b)	Unit - I	CO1	K3		
17. a)	Unit - II	CO2	K4		
OR					
17. b)	Unit - II	CO2	K4		
18. a)	Unit - III	CO3	K3		
OR					
18. b)	Unit - III	CO3	K3		
19. a)	Unit - IV	CO4	K4		
OR					
19. b)	Unit - IV	CO4	K4		
20. a)	Unit - V	CO5	K4		
OR					
20. b)	Unit - V	CO5	K4		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	REAL ANALYSIS - II			
<b>Course Code</b>	24PMTCC22	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	CORE	6	-	5
<b>COURSE OBJECTIVES:</b>				
➤ To introduce measure on the real line, Lebesgue measurability and integrability, Fourier Series and Integrals, in-depth study in multivariable calculus.				
<b>UNIT – I Measure on the Real line</b>				<b>18</b>
Lebesgue Outer Measure - Measurable sets - Regularity - Measurable Functions - Borel and Lebesgue Measurability.				
<b>UNIT – II Integration of Functions of a Real variable</b>				<b>18</b>
Integration of Non- negative functions - The General Integral - Riemann and Lebesgue Integrals				
<b>UNIT - III Fourier Series and Fourier Integrals</b>				<b>18</b>
Introduction - Orthogonal system of functions - The theorem on best approximation - The Fourier series of a function relative to an orthonormal system - Properties of Fourier Coefficients - The Riesz-Fischer Theorem - The convergence and representation problems in for trigonometric series - The Riemann - Lebesgue Lemma - The Dirichlet Integrals - An integral representation for the partial sums of Fourier series - Riemann's localization theorem - Sufficient conditions for convergence of a Fourier series at a particular point – Cesaro-summability of Fourier series- Consequences of Fejes's theorem - The Weierstrass approximation theorem				
<b>UNIT – IV Multivariable Differential Calculus</b>				<b>18</b>
Introduction - The Directional derivative - Directional derivative and continuity - The total derivative - The total derivative expressed in terms of partial derivatives - The matrix of linear function - The Jacobian matrix - The chain rule - Matrix form of chain rule - The mean - value theorem for differentiable functions - A sufficient condition for differentiability - A sufficient condition for equality of mixed partial derivatives - Taylor's theorem for functions of $\mathbb{R}^n$ to $\mathbb{R}^1$				
<b>UNIT - V Implicit Functions and Extremum Problems</b>				<b>18</b>
Functions with non-zero Jacobian determinants – The inverse function theorem-The Implicit function theorem-Extrema of real valued functions of severable variables-Extremum problems with side conditions.				
<b>Total Lecture Hours</b>				<b>90</b>



**BOOKS FOR STUDY:**

- G. de Barra, *Measure Theory and Integration*, Wiley Eastern Ltd., New Delhi, 1981. (for Units I and II)

**UNIT I : Chapter - 2 Sec 2.1 to 2.5**

**UNIT II: Chapter - 3 Sec 3.1,3.2 and 3.4**

- Tom M.Apostol : *Mathematical Analysis*, 2<sup>nd</sup> Edition, Addison-Wesley Publishing Company Inc. New York, 1974. (for Units III, IV and V)

**UNIT III: Chapter 11 : Sections 11.1 to 11.15**

**UNIT IV: Chapter 12 : Section 12.1 to 12.14**

**UNIT V: Chapter 13 : Sections 13.1 to 13.7**

**BOOKS FOR REFERENCES:**

- Burkill,J.C.The Lebesgue Integral, Cambridge University Press, 1951.
- Munroe,M.E.Measure and Integration. Addison-Wesley, Mass.1971.
- Roydon,H.L.Real Analysis, Macmillan Pub. Company, New York, 1988.
- Rudin, W. Principles of Mathematical Analysis, McGraw Hill Company, New York,1979.
- Malik,S.C. and Savita Arora. Mathematical Analysis, Wiley Eastern Limited. New Delhi, 1991.
- Sanjay Arora and Bansil Lal, Introduction to Real Analysis, Satya Prakashan, New Delhi, 1991

**WEB RESOURCES:**

- ❖ <http://mathforum.org>,
- ❖ <http://ocw.mit.edu/oc>.
- ❖ [www/Mathematics](http://www.mathematics)
- ❖ <http://www.opensource.org>

<b>Nature of Course</b>	EMPLOYABILITY		✓	SKILL ORIENTED		ENTREPRENEURSHIP		
<b>Curriculum Relevance</b>	LOCAL		REGIONAL		NATIONAL	✓	GLOBAL	
<b>Changes Made in the Course</b>	Percentage of Change			No Changes Made		✓	New Course	

**\* Treat 20% as each unit (20\*5=100%) and calculate the percentage of change for the course.**

<b>COURSE OUTCOMES:</b>	<b>K LEVEL</b>
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After studying this course, the students will be able to:

<b>CO1</b>	Understand and describe the basic concepts of Fourier series and Fourier integrals with respect to orthogonal system.	<b>K1 to K5</b>
<b>CO2</b>	Analyze the representation and convergence problems of Fourier series.	<b>K1 to K5</b>
<b>CO3</b>	Analyze and evaluate the difference between transforms of various functions.	<b>K1 to K5</b>
<b>CO4</b>	Formulate and evaluate complex contour integrals directly and by the fundamental theorem.	<b>K1 to K5</b>
<b>CO5</b>	Apply the Cauchy integral theorem in its various versions to compute contour integration	<b>K1 to K5</b>

<b>MAPPING WITH PROGRAM OUTCOMES:</b>										
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CO/PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
<b>CO1</b>	<b>3</b>	<b>1</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>3</b>				
<b>CO2</b>	<b>2</b>	<b>1</b>	<b>3</b>	<b>1</b>	<b>3</b>	<b>3</b>				
<b>CO3</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>1</b>	<b>3</b>	<b>3</b>				
<b>CO4</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>3</b>				
<b>CO5</b>	<b>3</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>3</b>	<b>3</b>				

**S- STRONG**

**M – MEDIUM**

**L - LOW**

<b>CO / PO MAPPING:</b>						
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COS	PSO1	PSO2	PSO3	PSO4	PSO5
<b>CO 1</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 2</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 3</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 4</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 5</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

<b>LESSON PLAN:</b>			
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UNIT	REAL ANALYSIS II	HRS	PEDAGOGY
<b>I</b>	Lebesgue Outer Measure - Measurable sets - Regularity - Measurable Functions - Borel and Lebesgue Measurability	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>II</b>	Integration of Non- negative functions - The General Integral - Riemann and Lebesgue Integrals	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>III</b>	Introduction - Orthogonal system of functions - The theorem on best approximation - The Fourier series of a function relative to an orthonormal system - Properties of Fourier Coefficients - The Riesz-Fischer Theorem - The convergence and representation problems in for trigonometric series - The Riemann - Lebesgue Lemma - The Dirichlet Integrals - An integral representation for the partial sums of Fourier series - Riemann's localization theorem - Sufficient conditions for convergence of a Fourier series at a particular point – Cesaro summability of Fourier series- Consequences of Fejes's theorem - The Weierstrass approximation theorem	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>IV</b>	Introduction - The Directional derivative - Directional derivative and continuity - The total derivative - The total derivative expressed in terms of partial derivatives - The matrix of linear function - The Jacobian matrix - The chain rule - Matrix form of chain rule - The mean - value theorem for differentiable functions - A sufficient condition for differentiability - A sufficient condition for equality of mixed partial derivatives - Taylor's theorem for functions of $R^n$ to $R^1$	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>V</b>	Functions with non-zero Jacobian determinants – The inverse function theorem-The Implicit function theorem-Extrema of real valued functions of severable variables-Extremum problems with side conditions.	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>Learning Outcome Based Education &amp; Assessment (LOBE)</b>						
<b>Formative Examination - Blue Print</b>						
<b>Articulation Mapping – K Levels with Course Outcomes (COs)</b>						
Internal	Cos	K Level	Section A		Section B Either or Choice	Section C Either or Choice
			MCQs			
			No. of Questions	K - Level		
CI	CO1	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AI	CO2	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
CI	CO3	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AII	CO4	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
<b>Question Pattern CIA I &amp; II</b>		<b>No. of Questions to be asked</b>	4		4	4
		<b>No. of Questions to be answered</b>	4		2	2
		<b>Marks for each question</b>	1		5	8
		<b>Total Marks for each section</b>	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100

**NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.**

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions				<b>PART – A</b>	
				<b>(10 x 1 = 10 Marks)</b>	
1.	Unit - I	CO1	K1	a)	b)
				c)	d)
2.	Unit - I	CO1	K2	a)	b)
				c)	d)
3.	Unit - II	CO2	K1	a)	b)
				c)	d)
4.	Unit - II	CO2	K2	a)	b)
				c)	d)
5.	Unit - III	CO3	K1	a)	b)
				c)	d)
6.	Unit - III	CO3	K2	a)	b)
				c)	d)
7.	Unit - IV	CO4	K1	a)	b)
				c)	d)
8.	Unit - IV	CO4	K2	a)	b)
				c)	d)
9.	Unit - V	CO5	K1	a)	b)
				c)	d)
10.	Unit - V	CO5	K2	a)	b)
				c)	d)

Answer ALL the questions

**PART – B**

**(5 x 5 = 25 Marks)**

11. a)	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>	
<b>OR</b>				
11. b)	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>	
12. a)	<b>Unit - II</b>	<b>CO2</b>	<b>K3</b>	
<b>OR</b>				
12. b)	<b>Unit - II</b>	<b>CO2</b>	<b>K3</b>	
13. a)	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	
<b>OR</b>				
13. b)	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	
14. a)	<b>Unit - IV</b>	<b>CO4</b>	<b>K3</b>	
<b>OR</b>				
14. b)	<b>Unit - IV</b>	<b>CO4</b>	<b>K3</b>	
15. a)	<b>Unit - V</b>	<b>CO5</b>	<b>K3</b>	
<b>OR</b>				
15. b)	<b>Unit - V</b>	<b>CO5</b>	<b>K3</b>	

Answer <b>ALL</b> the questions				<b>PART – C</b>	<b>(5 x 8 = 40 Marks)</b>
16. a)	<b>Unit - I</b>	<b>CO1</b>	<b>K3</b>		
<b>OR</b>					
16. b)	<b>Unit - I</b>	<b>CO1</b>	<b>K3</b>		
17. a)	<b>Unit - II</b>	<b>CO2</b>	<b>K4</b>		
<b>OR</b>					
17. b)	<b>Unit - II</b>	<b>CO2</b>	<b>K4</b>		
18. a)	<b>Unit - III</b>	<b>CO3</b>	<b>K3</b>		
<b>OR</b>					
18. b)	<b>Unit - III</b>	<b>CO3</b>	<b>K3</b>		
19. a)	<b>Unit - IV</b>	<b>CO4</b>	<b>K4</b>		
<b>OR</b>					
19. b)	<b>Unit - IV</b>	<b>CO4</b>	<b>K4</b>		
20. a)	<b>Unit - V</b>	<b>CO5</b>	<b>K4</b>		
<b>OR</b>					
20. b)	<b>Unit - V</b>	<b>CO5</b>	<b>K4</b>		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	PARTIAL DIFFERENTIAL EQUATIONS			
<b>Course Code</b>	24PMTCC23	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	Core	6	-	4
<b>COURSE OBJECTIVES:</b>				
➤ To classify the second order partial differential equations and to study Cauchy problem, method of separation of variables, boundary value problems				
<b>UNIT – I Mathematical Models and Classification of second order equation</b>		<b>18</b>		
Classical equations-Vibrating string – Vibrating membrane – waves in elastic medium – Conduction of heat in solids – Gravitational potential – Second order equations in two independent variables – canonical forms – equations with constant coefficients – general solution				
<b>UNIT – II Cauchy Problem</b>		<b>18</b>		
The Cauchy problem – Cauchy-Kowalewsky theorem – Homogeneous wave equation – Initial Boundary value problem- Non-homogeneous boundary conditions – Finite string with fixed ends – Non-homogeneous wave equation – Riemann method – Goursat problem – spherical wave equation – cylindrical wave equation.				
<b>UNIT - III Method of separation of variables</b>		<b>18</b>		
Separation of variable- Vibrating string problem – Existence and uniqueness of solution of vibrating string problem - Heat conduction problem – Existence and uniqueness of solution of heat conduction problem – Laplace and beam equations				
<b>UNIT – IV Boundary Value Problems</b>		<b>18</b>		
Boundary value problems – Maximum and minimum principles – Uniqueness and continuity theorem – Dirichlet Problem for a circle, a circular annulus, a rectangle – Dirichlet problem involving Poisson equation – Neumann problem for a circle and a rectangle.				
<b>UNIT - V Green's Function</b>		<b>18</b>		
The Delta function – Green's function – Method of Green's function – Dirichlet Problem for the Laplace and Helmholtz operators – Method of images and eigen functions – Higher dimensional problem – Neumann Problem.				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

- TynMyint-U and Lokenath Debnath, *Partial Differential Equations for Scientists and Engineers* (Third Edition), North Hollan, New York, 1987.

**UNIT I : Chapter 2 : Sections 2.1 to 2.6**

**Chapter 3 : Sections 3.1 to 3.4 (Omit 3.5)**

**UNIT II: Chapter 4 : Sections 4.1 to 4.11**

**UNIT III: Chapter 6 : Sections 6.1 to 6.6 (Omit section 6.7)**

**UNIT IV : Chapter 8 : Sections 8.1 to 8.9**

**UNIT V: Chapter 10 : Section 10.1 to 10.9**

**BOOKS FOR REFERENCES:**

- M.M.Smirnov, *Second Order partial Differential Equations*, Leningrad, 1964.
- I.N.Sneddon, *Elements of Partial Differential Equations*, McGraw Hill, New Delhi, 1983.
- R. Dennemeyer, *Introduction to Partial Differential Equations and Boundary Value Problems*, McGraw Hill, New York, 1968.
- M.D.Raisinghania, *Advanced Differential Equations*, S.Chand & Company Ltd., New Delhi, 2001.
- S, Sankar Rao, *Partial Differential Equations*, 2<sup>nd</sup> Edition, Prentice Hall of India, New Delhi. 2004

**WEB RESOURCES:**

- ❖ <http://mathforum.org>,
- ❖ <http://ocw.mit.edu/ocwweb/Mathematics>,
- ❖ <http://www.opensource.org>, [www.mathpages.com](http://www.mathpages.com)

<b>Nature of Course</b>	EMPLOYABILITY	✓	SKILL ORIENTED		ENTREPRENEURSHIP	
<b>Curriculum Relevance</b>	LOCAL	REGIONAL	NATIONAL	✓	GLOBAL	
<b>Changes Made in the Course</b>	Percentage of Change		No Changes Made	✓	New Course	

**\* Treat 20% as each unit (20\*5=100%) and calculate the percentage of change for the course.**

**COURSE OUTCOMES:****K LEVEL**

**After studying this course, the students will be able to:**

<b>CO1</b>	To understand and classify second order equations and find general solutions	<b>K1 to K5</b>
<b>CO2</b>	To analyse and solve wave equations in different polar coordinates	<b>K1 to K5</b>
<b>CO3</b>	To solve Vibrating string problem, Heat conduction problem, to identify and solve Laplace and beam equations	<b>K1 to K5</b>
<b>CO4</b>	To apply maximum and minimum principle's and solve Dirichlet, Neumann problems for various boundary conditions	<b>K1 to K5</b>
<b>CO5</b>	To apply Green's function and solve Dirichlet, Laplace problems, to apply Helmholtz operation and to solve Higher dimensional problem	<b>K1 to K5</b>



**MAPPING WITH PROGRAM OUTCOMES:**

CO/PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	3	1	3	2	3	3				
CO2	2	1	3	1	3	3				
CO3	3	2	3	1	3	3				
CO4	1	2	3	2	3	3				
CO5	3	1	2	3	3	3				

**S- STRONG**

**M – MEDIUM**

**L - LOW**

**CO / PO MAPPING:**

COS	PSO1	PSO2	PSO3	PSO4	PSO5
CO 1	3	2	1		
CO 2	3	2	1		
CO 3	3	2	1		
CO 4	3	2	1		
CO 5	3	2	1		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

**LESSON PLAN:**

UNIT	PARTIAL DIFFERENTIAL EQUATIONS	HRS	PEDAGOGY
<b>I</b>	Classical equations-Vibrating string – Vibrating membrane – waves in elastic medium – Conduction of heat in solids – Gravitational potential – Second order equations in two independent variables – canonical forms – equations with constant coefficients – general solution	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>II</b>	The Cauchy problem – Cauchy-Kowalewsky theorem – Homogeneous wave equation – Initial Boundary value problem- Non-homogeneous boundary conditions – Finite string with fixed ends – Non-homogeneous wave equation – Riemann method – Goursat problem – spherical wave equation – cylindrical wave equation.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>III</b>	Separation of variable- Vibrating string problem – Existence and uniqueness of solution of vibrating string problem - Heat conduction problem – Existence and uniqueness of solution of heat conduction problem – Laplace and beam equations	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>IV</b>	Boundary value problems – Maximum and minimum principles – Uniqueness and continuity theorem – Dirichlet Problem for a circle , a	<b>18</b>	<b>Chalk &amp;</b>

	circular annulus, a rectangle – Dirichlet problem involving Poisson equation – Neumann problem for a circle and a rectangle.		<b>Talk</b>
<b>V</b>	The Delta function – Green’s function – Method of Green’s function – Dirichlet Problem for the Laplace and Helmholtz operators – Method of images and eigen functions – Higher dimensional problem – Neumann Problem	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>Learning Outcome Based Education &amp; Assessment (LOBE)</b>						
<b>Formative Examination - Blue Print</b>						
<b>Articulation Mapping – K Levels with Course Outcomes (COs)</b>						
<b>Internal</b>	<b>Cos</b>	<b>K Level</b>	<b>Section A</b>		<b>Section B Either or Choice</b>	<b>Section C Either or Choice</b>
			<b>MCQs</b>			
			<b>No. of Questions</b>	<b>K - Level</b>		
<b>CI</b>	<b>CO1</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AI</b>	<b>CO2</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>CI</b>	<b>CO3</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AII</b>	<b>CO4</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>Question Pattern CIA I &amp; II</b>		<b>No. of Questions to be asked</b>	4		4	4
		<b>No. of Questions to be answered</b>	4		2	2
		<b>Marks for each question</b>	1		5	8
		<b>Total Marks for each section</b>	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100

**NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.**

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions				<b>PART – A</b>	
				<b>(10 x 1 = 10 Marks)</b>	
1.	Unit - I	CO1	K1	a)	b)
				c)	d)
2.	Unit - I	CO1	K2	a)	b)
				c)	d)
3.	Unit - II	CO2	K1	a)	b)
				c)	d)
4.	Unit - II	CO2	K2	a)	b)
				c)	d)
5.	Unit - III	CO3	K1	a)	b)
				c)	d)
6.	Unit - III	CO3	K2	a)	b)
				c)	d)
7.	Unit - IV	CO4	K1	a)	b)
				c)	d)
8.	Unit - IV	CO4	K2	a)	b)
				c)	d)
9.	Unit - V	CO5	K1	a)	b)
				c)	d)
10.	Unit - V	CO5	K2	a)	b)
				c)	d)

Answer ALL the questions				PART – B	(5 x 5 = 25 Marks)
11. a)	Unit - I	CO1	K2		
OR					
11. b)	Unit - I	CO1	K2		
12. a)	Unit - II	CO2	K3		
OR					
12. b)	Unit - II	CO2	K3		
13. a)	Unit - III	CO3	K2		
OR					
13. b)	Unit - III	CO3	K2		
14. a)	Unit - IV	CO4	K3		
OR					
14. b)	Unit - IV	CO4	K3		
15. a)	Unit - V	CO5	K3		
OR					
15. b)	Unit - V	CO5	K3		

Answer ALL the questions				PART – C	(5 x 8 = 40 Marks)
16. a)	Unit - I	CO1	K3		
OR					
16. b)	Unit - I	CO1	K3		
17. a)	Unit - II	CO2	K4		
OR					
17. b)	Unit - II	CO2	K4		
18. a)	Unit - III	CO3	K3		
OR					
18. b)	Unit - III	CO3	K3		
19. a)	Unit - IV	CO4	K4		
OR					
19. b)	Unit - IV	CO4	K4		
20. a)	Unit - V	CO5	K4		
OR					
20. b)	Unit - V	CO5	K4		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	NUMERICAL ANALYSIS			
<b>Course Code</b>	24PMTEC21	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	ELECTIVE	5	-	3
<b>COURSE OBJECTIVES:</b>				
<ul style="list-style-type: none"><li>➤ To develop Numerical computational skills.</li><li>➤ To practice Numerical computational applications.</li><li>➤ To introduce difference equations and recurrence equations.</li><li>➤ To demonstrate understanding and implementation of numerical solution of algorithms based for employability</li><li>➤ To find the errors in the approximation</li></ul>				
<b>UNIT – I</b>				<b>18</b>
Bisection method – Iteration method (approximation method) based on first degree equation, second degree equation.				
<b>UNIT – II</b>				<b>18</b>
Direct methods: forward substitution method, back substitution method, Cramer rule, Gauss elimination method, Gauss Jordan method – triangulation method – LU decomposition– Cholesky method – Partition method.				
<b>UNIT - III</b>				<b>18</b>
Iterative methods - Jacobi iteration methods, Gauss-Seidel iteration methods, Similarity transformation – Eigen values – Eigen vectors –Jacobi method for symmetric matrices.				
<b>UNIT – IV</b>				<b>18</b>
Lagrange’s and Newton Interpolation, Finite Difference Operators, Interpolating Polynomials using Finite Differences, Hermite Interpolation.				
<b>UNIT - V</b>				<b>18</b>
Numerical Differentiation, Partial Differentiation, Numerical Integration, Methods based on Interpolation, Composite Integration methods.				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

- M.K.Jain, S.R.K.Iyengar, R.K.Jain, **Numerical Methods for scientific and Engineering computation** – 4th edition, New age international Pvt limited, New Delhi, 2009.

Unit I - Chapter 2 : Section 2.1-2.4 and 2.5

Unit II - Chapter 3 : Section 3.1, 3.2

Unit III - Chapter 3 : Section 3.4, 3.5 and 3.7

Unit IV - Chapter 4 : Section 4.1 – 4.5

Unit V - Chapter 5 : Section 5.1, 5.2, 5.5 - 5.7, 5.9.

**BOOKS FOR REFERENCES:**

- G.Shankar Rao, **Numerical Analysis**, New Age International publishers, New Delhi,1997.
- Rainer Kress, **Numerical Analysis**, Springer international Edition, New Delhi, 2010.
- S.R.K.Iyengar ,R.K.Jain ,**Numerical Methods**, , New age international Pvt limited, New Delhi, 2008.

**WEB RESOURCES:**

- ❖ <http://www.ece.mcmaster.ca/~xwu/part6.pdf>
- ❖ <http://www.cis.upenn.edu/~cis515/cis515-12-sl2.pdf>
- ❖ [https://wiki.math.ntnu.no/\\_media/tma4215/2012h/note.pdf](https://wiki.math.ntnu.no/_media/tma4215/2012h/note.pdf)

<b>Nature of Course</b>	EMPLOYABILITY		✓	SKILL ORIENTED		ENTREPRENEURSHIP		
<b>Curriculum Relevance</b>	LOCAL		REGIONAL		NATIONAL	✓	GLOBAL	
<b>Changes Made in the Course</b>	Percentage of Change			No Changes Made		✓	New Course	
<b>* Treat 20% as each unit (20*5=100%) and calculate the percentage of change for the course.</b>								

<b>COURSE OUTCOMES:</b>		<b>K LEVEL</b>
<b>After studying this course, the students will be able to:</b>		
<b>CO1</b>	Demonstrate the understanding of direct methods and iterative methods for equations	<b>K1 to K5</b>
<b>CO2</b>	Apply proper methods for solving transcendental, algebraic and system of equations	<b>K1 to K5</b>
<b>CO3</b>	Evaluate interpolation and extrapolation using tabular values	<b>K1 to K5</b>
<b>CO4</b>	Associate tabular values with integration and differentiation	<b>K1 to K5</b>
<b>CO5</b>	Use iterative methods for PDE	<b>K1 to K5</b>

<b>MAPPING WITH PROGRAM OUTCOMES:</b>										
<b>CO/PO</b>	<b>PO1</b>	<b>PO2</b>	<b>PO3</b>	<b>PO4</b>	<b>PO5</b>	<b>PO6</b>	<b>PO7</b>	<b>PO8</b>	<b>PO9</b>	<b>PO10</b>
<b>CO1</b>	<b>3</b>	<b>3</b>	<b>3</b>	<b>1</b>	<b>1</b>	<b>1</b>				
<b>CO2</b>	<b>3</b>	<b>3</b>	<b>2</b>	<b>2</b>	<b>1</b>	<b>-</b>				
<b>CO3</b>	<b>3</b>	<b>3</b>	<b>3</b>	<b>1</b>	<b>1</b>	<b>1</b>				
<b>CO4</b>	<b>3</b>	<b>3</b>	<b>2</b>	<b>2</b>	<b>1</b>	<b>-</b>				
<b>CO5</b>	<b>3</b>	<b>3</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>1</b>				

**S- STRONG** **M – MEDIUM** **L - LOW**

<b>CO / PO MAPPING:</b>					
<b>COS</b>	<b>PSO1</b>	<b>PSO2</b>	<b>PSO3</b>	<b>PSO4</b>	<b>PSO5</b>
<b>CO 1</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 2</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 3</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 4</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 5</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

<b>LESSON PLAN:</b>			
<b>UNIT</b>	<b>NUMERICAL ANALYSIS</b>	<b>HRS</b>	<b>PEDAGOGY</b>
<b>I</b>	Bisection method – Iteration method (approximation method) based on first degree equation, second degree equation.	<b>18</b>	<b>Chalk &amp; Talk, PPT</b>
<b>II</b>	Direct methods: forward substitution method, back substitution method, Cramer rule, Gauss elimination method, Gauss Jordan method – triangulation method – LU decomposition– Cholesky method – Partition method.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>III</b>	Iterative methods - Jacobi iteration methods, Gauss-Seidel iteration methods, Similarity transformation – Eigen values – Eigen vectors –	<b>18</b>	<b>Chalk &amp; Talk</b>



	Jacobi method for symmetric matrices.		
<b>IV</b>	Lagrange's and Newton Interpolation, Finite Difference Operators, Interpolating Polynomials using Finite Differences, Hermite Interpolation.	<b>18</b>	<b>Chalk &amp; Talk, PPT</b>
<b>V</b>	Numerical Differentiation, Partial Differentiation, Numerical Integration, Methods based on Interpolation, Composite Integration methods.	<b>18</b>	<b>Chalk &amp; Talk</b>

<b>Learning Outcome Based Education &amp; Assessment (LOBE)</b>						
<b>Formative Examination - Blue Print</b>						
<b>Articulation Mapping – K Levels with Course Outcomes (COs)</b>						
<b>Internal</b>	<b>Cos</b>	<b>K Level</b>	<b>Section A</b>		<b>Section B Either or Choice</b>	<b>Section C Either or Choice</b>
			<b>MCQs</b>			
			<b>No. of Questions</b>	<b>K - Level</b>		
<b>CI</b>	<b>CO1</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AI</b>	<b>CO2</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>CI</b>	<b>CO3</b>	<b>K1 – K5</b>	2	K2	2(K2,K2)	2(K3,K3)
<b>AII</b>	<b>CO4</b>	<b>K1 – K5</b>	2	K2	2(K3,K3)	2(K4,K4)
<b>Question Pattern CIA I &amp; II</b>		<b>No. of Questions to be asked</b>	4		4	4
		<b>No. of Questions to be answered</b>	4		2	2
		<b>Marks for each question</b>	1		5	8
		<b>Total Marks for each section</b>	4		10	16

Distribution of Marks with K Level CIA I & CIA II							
	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	46.4
	K4			16	16	28.6	28.6
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	46.4
	K4		10	16	26	46.4	46.4
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)						
S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100

**NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.**

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer ALL the questions <b>PART – A</b> (10 x 1 = 10 Marks)					
1.	Unit - I	CO1	K1	a)	b)
				c)	d)
2.	Unit - I	CO1	K2	a)	b)
				c)	d)
3.	Unit - II	CO2	K1	a)	b)
				c)	d)
4.	Unit - II	CO2	K2	a)	b)
				c)	d)
5.	Unit - III	CO3	K1	a)	b)
				c)	d)
6.	Unit - III	CO3	K2	a)	b)
				c)	d)
7.	Unit - IV	CO4	K1	a)	b)
				c)	d)
8.	Unit - IV	CO4	K2	a)	b)
				c)	d)
9.	Unit - V	CO5	K1	a)	b)
				c)	d)
10.	Unit - V	CO5	K2	a)	b)
				c)	d)

Answer ALL the questions <b>PART – B</b> (5 x 5 = 25 Marks)					
11. a)	Unit - I	CO1	K2		
<b>OR</b>					

11. b)	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>	
12. a)	<b>Unit - II</b>	<b>CO2</b>	<b>K3</b>	
<b>OR</b>				
12. b)	<b>Unit - II</b>	<b>CO2</b>	<b>K3</b>	
13. a)	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	
<b>OR</b>				
13. b)	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	
14. a)	<b>Unit - IV</b>	<b>CO4</b>	<b>K3</b>	
<b>OR</b>				
14. b)	<b>Unit - IV</b>	<b>CO4</b>	<b>K3</b>	
15. a)	<b>Unit - V</b>	<b>CO5</b>	<b>K3</b>	
<b>OR</b>				
15. b)	<b>Unit - V</b>	<b>CO5</b>	<b>K3</b>	

Answer <b>ALL</b> the questions				<b>PART – C</b>	<b>(5 x 8 = 40 Marks)</b>
16. a)	<b>Unit - I</b>	<b>CO1</b>	<b>K3</b>		
<b>OR</b>					
16. b)	<b>Unit - I</b>	<b>CO1</b>	<b>K3</b>		
17. a)	<b>Unit - II</b>	<b>CO2</b>	<b>K4</b>		
<b>OR</b>					
17. b)	<b>Unit - II</b>	<b>CO2</b>	<b>K4</b>		
18. a)	<b>Unit - III</b>	<b>CO3</b>	<b>K3</b>		
<b>OR</b>					
18. b)	<b>Unit - III</b>	<b>CO3</b>	<b>K3</b>		
19. a)	<b>Unit - IV</b>	<b>CO4</b>	<b>K4</b>		
<b>OR</b>					
19. b)	<b>Unit - IV</b>	<b>CO4</b>	<b>K4</b>		
20. a)	<b>Unit - V</b>	<b>CO5</b>	<b>K4</b>		
<b>OR</b>					
20. b)	<b>Unit - V</b>	<b>CO5</b>	<b>K4</b>		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	RESOURCE MANAGEMENT TECHNIQUES			
<b>Course Code</b>	24PMTEC22	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	ELECTIVE	5	-	3
<b>COURSE OBJECTIVES:</b>				
<ul style="list-style-type: none"><li>➤ To familiarize various decisions– making tools.</li><li>➤ To solve optimization problems.</li><li>➤ To introduce the application on inventory control system and etc.</li><li>➤ To identify the resources required for a project and generate a plan and work schedule.</li><li>➤ To learn about queuing models.</li></ul>				
<b>UNIT – I</b>				<b>18</b>
Network definitions- Minimal Spanning Tree Algorithm-Shortest route problem-Maximal Flow Model - CPM and PERT.				
<b>UNIT – II</b>				<b>18</b>
Recursive nature of computations in DP - Forward and Backward recursion - Selected DP applications. General inventory models – Static Economic Order Quantity(EOQ) models.				
<b>UNIT - III</b>				<b>18</b>
Decision making under certainty-Analytic Hierarchy Process(AHP)-Decision making under risk- Decision under uncertainty-Game theory.				
<b>UNIT – IV</b>				<b>18</b>
Queuing systems – Elements of Queuing model – Role of Exponential Distribution – Pure Birth and Death Models – Generalized Poisson Queuing Models – Specialized Poisson Queues.				
<b>UNIT - V</b>				<b>18</b>
Unconstrained Problems – Necessary and Sufficient Conditions- Newton – Raphson Method - Constrained Problems – Equality Constraints- Inequality Constraints- Karush-Kuhn-Tucker Conditions.				
<b>Total Lecture Hours</b>				<b>90</b>

**BOOKS FOR STUDY:**

- Hamdy A. Taha, **Operations Research** – An introduction, 8<sup>th</sup> Edition, PHI, New Delhi.
  - Unit I- Chapter 6: sections 6.1 to6.5
  - Unit II - Chapter 10: sections 10.1 to10.3  
Chapter 11:sections 11.1 to 11.3
  - Unit III - Chapter 13:sections 13.1 to 13.4
  - Unit IV - Chapter 15:sections 15.1 to 15.6
  - Unit V - Chapter 18: sections 18.1 to18.2

**BOOKS FOR REFERENCES:**

- KantiSwarup , P.K. Gupta and Man Mohan, “**Operations Research**” , Sultan Chand & sons Publications, Reprint 2006, NewDelhi.
- Harvey M. Wagner, “**Principles of Operations Research**”, Second Edition, Prentice Hall of Pvt Ltd, 1998, NewDelhi.
- Prem Kumar Gupta and D.S.Hira, “**Operations Research**”, S.Chand Publications, 2009, New Delhi.

**WEB RESOURCES:**

- ❖ <https://nptel.ac.in/courses/111/105/111105100/>
- ❖ <https://nptel.ac.in/courses/111/104/111104071/>
- ❖ <http://apmonitor.com/me575/>

<b>Nature of Course</b>	EMPLOYABILITY		✓	SKILL ORIENTED		ENTREPRENEURSHIP		
<b>Curriculum Relevance</b>	LOCAL	REGIONAL		NATIONAL		GLOBAL		✓
<b>Changes Made in the Course</b>	Percentage of Change			No Changes Made		✓	New Course	

**\* Treat 20% as each unit (20\*5=100%) and calculate the percentage of change for the course.**

**COURSE OUTCOMES:****K LEVEL**

After studying this course, the students will be able to:

<b>CO1</b>	Identify various decisions– making tools.	<b>K1 to K5</b>
<b>CO2</b>	Analyze various models in inventory system.	<b>K1 to K5</b>
<b>CO3</b>	Apply suitable method in game theory.	<b>K1 to K5</b>
<b>CO4</b>	Explain Poisson Queuing Models	<b>K1 to K5</b>
<b>CO5</b>	Classify the constrained and unconstrained Problems	<b>K1 to K5</b>

**MAPPING WITH PROGRAM OUTCOMES:**

CO/PO	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
<b>CO1</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>3</b>				
<b>CO2</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>2</b>	<b>2</b>	<b>3</b>				
<b>CO3</b>	<b>3</b>	<b>2</b>	<b>3</b>	<b>2</b>	<b>2</b>	<b>3</b>				
<b>CO4</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>3</b>				
<b>CO5</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>2</b>	<b>3</b>				

**S- STRONG****M – MEDIUM****L - LOW**

**CO / PO MAPPING:**

<b>COS</b>	<b>PSO1</b>	<b>PSO2</b>	<b>PSO3</b>	<b>PSO4</b>	<b>PSO5</b>
<b>CO 1</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 2</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 3</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 4</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>CO 5</b>	<b>3</b>	<b>2</b>	<b>1</b>		
<b>WEIGHTAGE</b>	<b>15</b>	<b>10</b>	<b>5</b>		
<b>WEIGHTED PERCENTAGE OF COURSE CONTRIBUTION TO POS</b>	<b>3</b>	<b>2</b>	<b>1</b>		

**LESSON PLAN:**

<b>UNIT</b>	<b>RESOURCE MANAGEMENT TECHNIQUES</b>	<b>HRS</b>	<b>PEDAGOGY</b>
<b>I</b>	Network definitions- minimal spanning tree algorithm-Shortest route problem-maximal flow model - CPM and PERT.	<b>18</b>	<b>Chalk and Board, Virtual Class room, LCD projector</b>
<b>II</b>	Recursive nature of computations in DP - Forward and Backward recursion - Selected DP applications. General inventory models – Static Economic Order Quantity(EOQ) models	<b>18</b>	<b>Guest Lectures.</b>
<b>III</b>	Decision making under certainty-Analytic Hierarchy Process(AHP)- Decision making under risk- decision under uncertainty-Game theory.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>IV</b>	Queuing systems – Elements of Queuing model – Role of Exponential Distribution – Pure Birth and Death Models – Generalized Poisson Queuing Models – Specialized Poisson Queues.	<b>18</b>	<b>Chalk &amp; Talk</b>
<b>V</b>	Unconstrained Problems – Necessary and Sufficient Conditions- Newton – Raphson Method - Constrained Problems – Equality Constraints- Inequality Constraints- Karush-Kuhn-Tucker Conditions	<b>18</b>	<b>Chalk &amp; Talk</b>

**Learning Outcome Based Education & Assessment (LOBE)  
Formative Examination - Blue Print  
Articulation Mapping – K Levels with Course Outcomes (COs)**

Internal	Cos	K Level	Section A		Section B Either or Choice	Section C Either or Choice
			MCQs			
			No. of Questions	K - Level		
CI	CO1	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AI	CO2	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
CI	CO3	K1 – K5	2	K2	2(K2,K2)	2(K3,K3)
AII	CO4	K1 – K5	2	K2	2(K3,K3)	2(K4,K4)
Question Pattern CIA I & II		No. of Questions to be asked	4		4	4
		No. of Questions to be answered	4		2	2
		Marks for each question	1		5	8
		Total Marks for each section	4		10	16

**Distribution of Marks with K Level CIA I & CIA II**

	K Level	Section A (Multiple Choice Questions)	Section B (Either / Or Choice)	Section C (Either / Or Choice)	Total Marks	% of (Marks without choice)	Consolidate of %
CIA I	K1	2			2	3.6	25
	K2	2	10		12	21.4	
	K3		10	16	26	46.4	
	K4			16	16	28.6	
	K5						
	Marks	4	20	32	56	100	100
CIA II	K1	2			2	3.6	7.2
	K2	2			2	3.6	
	K3		10	16	26	46.4	
	K4		10	16	26	46.4	
	K5						
	Marks	4	20	32	56	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5** will be allotted for individual Assignment which carries five marks as part of CIA component.

**Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)**



S. No	Cos	K - Level	Section A (MCQs)		Section B (Either / or Choice) With K - LEVEL	Section C (Either / or Choice) With K - LEVEL
			No. of Questions	K – Level		
1	CO1	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
2	CO2	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
3	CO3	K1 – K5	2	K1,K2	2(K2,K2)	2(K3,K3)
4	CO4	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
5	CO5	K1 – K5	2	K1,K2	2(K3,K3)	2(K4,K4)
No. of Questions to be Asked			10		10	10
No. of Questions to be answered			10		10	5
Marks for each question			1		1	8
Total Marks for each section			10		10	40
(Figures in parenthesis denotes, questions should be asked with the given K level)						

Distribution of Marks with K Level						
K Level	Section A (Multiple Choice Questions)	Section B (Either or Choice)	Section C (Either/ or Choice)	Total Marks	% of (Marks without choice)	Consolidated %
K1	5			5	3.6	4
K2	5	20		25	17.8	18
K3		30	32	62	44.3	44
K4			48	48	34.3	34
Marks	10	50	80	140	100	100
NB: Higher level of performance of the students is to be assessed by attempting higher level of K levels.						

### Summative Examinations - Question Paper – Format

Q. No.	Unit	CO	K-level		
Answer <b>ALL</b> the questions			<b>PART – A</b>		<b>(10 x 1 = 10 Marks)</b>
1.	<b>Unit - I</b>	<b>CO1</b>	<b>K1</b>		
				a)	b)
				c)	d)
2.	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>		
				a)	b)
				c)	d)
3.	<b>Unit - II</b>	<b>CO2</b>	<b>K1</b>		
				a)	b)
				c)	d)
4.	<b>Unit - II</b>	<b>CO2</b>	<b>K2</b>		
				a)	b)
				c)	d)
5.	<b>Unit - III</b>	<b>CO3</b>	<b>K1</b>		
				a)	b)
				c)	d)
6.	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>		
				a)	b)
				c)	d)
7.	<b>Unit - IV</b>	<b>CO4</b>	<b>K1</b>		
				a)	b)
				c)	d)
8.	<b>Unit - IV</b>	<b>CO4</b>	<b>K2</b>		
				a)	b)
				c)	d)
9.	<b>Unit - V</b>	<b>CO5</b>	<b>K1</b>		
				a)	b)
				c)	d)
10.	<b>Unit - V</b>	<b>CO5</b>	<b>K2</b>		
				a)	b)
				c)	d)

Answer <b>ALL</b> the questions			<b>PART – B</b>		<b>(5 x 5 = 25 Marks)</b>
11. a)	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>		

<b>OR</b>				
11. b)	<b>Unit - I</b>	<b>CO1</b>	<b>K2</b>	
12. a)	<b>Unit - II</b>	<b>CO2</b>	<b>K3</b>	
<b>OR</b>				
12. b)	<b>Unit - II</b>	<b>CO2</b>	<b>K3</b>	
13. a)	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	
<b>OR</b>				
13. b)	<b>Unit - III</b>	<b>CO3</b>	<b>K2</b>	
14. a)	<b>Unit - IV</b>	<b>CO4</b>	<b>K3</b>	
<b>OR</b>				
14. b)	<b>Unit - IV</b>	<b>CO4</b>	<b>K3</b>	
15. a)	<b>Unit - V</b>	<b>CO5</b>	<b>K3</b>	
<b>OR</b>				
15. b)	<b>Unit - V</b>	<b>CO5</b>	<b>K3</b>	

Answer <b>ALL</b> the questions				<b>PART – C</b>	<b>(5 x 8 = 40 Marks)</b>
16. a)	<b>Unit - I</b>	<b>CO1</b>	<b>K3</b>		
<b>OR</b>					
16. b)	<b>Unit - I</b>	<b>CO1</b>	<b>K3</b>		
17. a)	<b>Unit - II</b>	<b>CO2</b>	<b>K4</b>		
<b>OR</b>					
17. b)	<b>Unit - II</b>	<b>CO2</b>	<b>K4</b>		
18. a)	<b>Unit - III</b>	<b>CO3</b>	<b>K3</b>		
<b>OR</b>					
18. b)	<b>Unit - III</b>	<b>CO3</b>	<b>K3</b>		
19. a)	<b>Unit - IV</b>	<b>CO4</b>	<b>K4</b>		
<b>OR</b>					
19. b)	<b>Unit - IV</b>	<b>CO4</b>	<b>K4</b>		
20. a)	<b>Unit - V</b>	<b>CO5</b>	<b>K4</b>		
<b>OR</b>					
20. b)	<b>Unit - V</b>	<b>CO5</b>	<b>K4</b>		



# MANNAR THIRUMALAI NAICKER COLLEGE (AUTONOMOUS)

## PG AND RESEARCH DEPARTMENT OF MATHEMATICS

FOR THOSE WHO JOINED IN 2024-2025 AND AFTER

<b>Course Name</b>	MATHEMATICS USING PYTHON			
<b>Course Code</b>	24PMTSP21	<b>L</b>	<b>P</b>	<b>C</b>
<b>Category</b>	SKILL	-	2	2
<b>COURSE OBJECTIVES:</b>				
<p>➤ To introduce the concepts and to develop working knowledge on the mathematical methods used to solve the problems using Python programming language.</p>				
<b>LIST OF PROGRAMMES</b>				
<ol style="list-style-type: none"><li>1. Find the factorial of a number n.</li><li>2. Find the sum of n terms of a series.</li><li>3. Find the nth power of a number x.</li><li>4. Divide two numbers and two polynomials.</li><li>5. Prepare a Python program to use arithmetic operators</li><li>6. Solve a system of two equations</li><li>7. Solve an ordinary differential equation using Range-Kutta method.</li><li>8. Solve an ordinary differential equation using Euler method</li></ol>				
<b>Total Lecture Hours</b>				<b>30</b>

### BOOKS FOR REFERENCES:

- P.R. Turner, T. Arildsen, K. Kavanagh, Applied Scientific Computing With Python, Springer International Publishing AG, part of Springer Nature, 2018
- J. M. STEWART, Python for Scientists, Cambridge University Press, 2014
- 2. C. Hill, Learning Scientific Programming with Python, Second Edition, Cambridge University Press, 2020, 2004.

### WEB RESOURCES:

- ❖ [https://www.w3schools.com/python/python\\_math.asp](https://www.w3schools.com/python/python_math.asp)



**LESSON PLAN:****MATHEMATICS USING PYTHON****LIST OF PROGRAMMES****HRS**

1. Find the factorial of a number n.
2. Find the sum of n terms of a series.
3. Find the nth power of a number x.
4. Divide two numbers and two polynomials.
5. Prepare a Python program to use arithmetic operators
6. Solve a system of two equations
7. Solve an ordinary differential equation using Range-Kutta method.
8. Solve an ordinary differential equation using Euler method

**30**

**Learning Outcome Based Education & Assessment (LOBE)  
Formative Examination - Blue Print  
Articulation Mapping – K Levels with Course Outcomes (COs)**

Internal	Cos	K Level	Syntax & Semantics	Programming principles	Concept Applications	Coding & Implementation	Debugging & Output
CIA	CO1	K1	5				
	CO2	K2		5			
	CO3	K3			5		
	CO4	K4				5	
	CO5	K4					5
Question Pattern CIA	No. of Questions to be asked		2	2	2	2	2
	No. of Questions to be answered		2	2	2	2	2
	Marks for each question		2.5	2.5	2.5	2.5	2.5
	Total Marks for each section		5	5	5	5	5

Distribution of Marks with K Level CIA									
	K Level	Syntax & Semantics	Programming principles	Concept Applications	Coding	Debugging & Output	Total Marks	% of Marks without choice)	Consolidated %
CIA	K1	5					5	20	20
	K2		5				5	20	20
	K3			5			5	20	20
	K4				5	5	10	40	40
	Marks						25	100	100

**K1-** Remembering and recalling facts with specific answers

**K2-** Basic understanding of facts and stating main ideas with general answers

**K3-** Application oriented- Solving Problems

**K4-** Examining, analyzing, presentation and make inferences with evidences

**CO5 will be allotted for individual Assignment which carries five marks as part of CIA component.**

Summative Examination – Blue Print Articulation Mapping – K Level with Course Outcomes (COs)							
S. No	Cos	K - Level	Syntax & Semantics	Programming principles	Concept Applications	Coding & Implementation	Debugging & Output
1	CO1	K1	15				
2	CO2	K2		15			
3	CO3	K3			15		
4	CO4	K4				15	
5	CO5	K4					15
No. of Questions to be Asked			2	2	2	2	2
No. of Questions to be answered			2	2	2	2	2
Marks for each question			7.5	7.5	7.5	7.5	7.5
Total Marks for each section			15	15	15	15	15
(Figures in parenthesis denotes, questions should be asked with the given K level)							

<b>Distribution of Marks with K Level CIA</b>									
	<b>K Level</b>	<b>Syntax &amp; Semantics</b>	<b>Program ming principles</b>	<b>Concept Applicatio ns</b>	<b>Codin g</b>	<b>Debuggi ng &amp; Output</b>	<b>Total Marks</b>	<b>% of (Mar ks without choic e)</b>	<b>Co nso lid ated %</b>
<b>CIA</b>	<b>K1</b>	15					<b>15</b>	<b>20</b>	<b>20</b>
	<b>K2</b>		15				<b>15</b>	<b>20</b>	<b>20</b>
	<b>K3</b>			15			15	20	20
	<b>K4</b>				15	15	30	40	40
	<b>Marks</b>						<b>75</b>	<b>100</b>	<b>100</b>